

# extended R documentation

of function `sorcering()`

from package '`sorcering`'

June 2, 2025

<b>Version</b>	1.2.0
<b>Title</b>	SORCERING: Soil ORganic Carbon & CN Ratio drIven Nitrogen modellinG framework
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<b>LazyData</b>	true
<b>Depends</b>	R (>= 3.5.0)
<b>License</b>	GLP (>= 2)
<b>Imports</b>	Rcpp (>= 1.0.6)
<b>LinkingTo</b>	Rcpp, RcppArmadillo
<b>NeedsCompilation</b>	yes

## Description

`SORCERING` can be used to model the fate of soil organic carbon (SOC) and soil organic nitrogen (SON) and to calculate N mineralisation rates. It provides a framework that numerically solves differential equations of SOC models based on first-order kinetics. An SOC model can be simply defined or a predefined existing SOC model can be chosen and then run to predict the temporal development of SOC. Beyond this, `SORCERING` determines the fluxes of SON and N mineralisation / immobilisation. Basic inputs are (1) the model parameters of a given SOC model expressed as the C transfer matrix (including information on decomposition and transfer rates between model pools), (2) either the initial distributions of C and N among model pools as a direct input or time series of at least three C and N measurement points with which these initial distributions can be calculated using linear regression, and (3) time series of C and N inputs and rate modifying environmental factors. In case a predefined SOC model is used, instead of model parameters and time series of rate modifying factors, model-specific environmental and stand data must be passed for the calculation of decomposition and transfer rates. Moreover, `SORCERING` provides the options to cover statistical uncertainties by using stochastic repetitions for many input data and parameters as well as to perform model spin-up runs. The fourth-order Runge-Kutta algorithm is used to numerically solve the system of differential equations.

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**Usage**

```
sorcering(
  A = NULL,
  tsteps = "monthly",
  C0 = NULL,
  N0 = NULL,
  Cin = NULL,
  Nin = NULL,
  Cin_wood = NULL,
  Nin_wood = NULL,
  wood_diam = NULL,
  xi = NULL,
  env_in = NULL,
  site = NULL,
  theta = NULL,
  theta_unc = NULL,
  theta_n_unc = 1,
  meas_data = NULL,
  A_sl = NULL,
  C0_sl = NULL,
  N0_sl = NULL,
  Cin_sl = NULL,
  Nin_sl = NULL,
  Cin_wood_sl = NULL,
  Nin_wood_sl = NULL,
  wood_diam_sl = NULL,
  xi_sl = NULL,
  env_in_sl = NULL,
  site_sl = NULL,
  sitelist = NULL,
  meas_data_sl = NULL,
  calcN = FALSE,
  calcNbalance = FALSE,
  calcN0 = FALSE,
  calcC0 = FALSE,
  calcCN_fast_init = FALSE,
  CTool_input_raw = FALSE,
  RothC_Cin4C0 = FALSE,
  RothC_dpmrpm = 1.439024,
  C0_fracts = NULL,
  multisite = FALSE,
  pooltypes = NULL,
  CN_fast_init = 40,
  CN_bio = 9,
  CN_spin = NULL,
  CN_fast_init_sl = NULL,
  CN_bio_sl = NULL,
  CN_spin_sl = NULL,
  init_info = FALSE,
  model = "",
  spinup = FALSE,
  t_spin = 2,
  t_spin_sl = 2)
```

## Arguments

In addition to the arguments descriptions below, Fig. 1 provides a visualisation of the list structure and Fig. 2 provides a visualisation of the content structure of the arguments.

<code>A</code>	square matrix. Transfer matrix typical for SOC modelling. Defines number of pools, decomposition and transfer rates. $n \times n$ elements with $n$ = number of pools. Diagonal values are decomposition rates [ $\text{yr}^{-1}$ ]. Off-diagonals represent the transfer between pools [ $\text{yr}^{-1}$ ]. Only used when <code>model</code> is <code>NULL</code> .
<code>tsteps</code>	character string indicating the type of simulation time steps. Valid options are "annually", "monthly" (recommended) or "weekly". Ensures that the rate modifying factors (passed through <code>xi</code> or used by a predefined model) are adjusted by dividing them by 1, 12, and 52 respectively. Furthermore ensures, that environment-specific information (passed through <code>env_in</code> ) takes into account the time reference of the modelling.
<code>C0</code>	either vector with a length equal to the number of pools or scalar. If vector, initial soil organic carbon per pool [ $\text{tC ha}^{-1}$ ]. If scalar, initial total soil organic carbon [ $\text{tC ha}^{-1}$ ]. In the latter case, either <code>model</code> must be selected or <code>C0_fracts</code> must be passed. If <code>NULL</code> , filled with zeros.
<code>N0</code>	vector with a length equal to the number of pools. Contains initial soil organic nitrogen per pool [ $\text{tN ha}^{-1}$ ]. If <code>NULL</code> , filled with zeros. Only used when <code>calcN</code> = <code>TRUE</code> and <code>calcN0</code> = <code>FALSE</code> .
<code>Cin</code>	either matrix with a number of columns equal to the number of pools and a number of rows corresponding to simulation time steps (if <code>spinup</code> = <code>FALSE</code> ) or spin-up reference period (if <code>spinup</code> = <code>TRUE</code> ), or list containing such matrices. If it is a list, each element of the list is expected to represent a stochastic repetition that covers input uncertainties. Then, the list must contain matrices of equal dimensions. Each matrix (or the one if modelling without uncertainties) must contain information about carbon input per pool and time step [ $\text{tC ha}^{-1}$ ]. When <code>CTool_input_raw</code> = <code>TRUE</code> , and <code>model</code> = "C-Tool" or <code>model</code> = "C-Tool-org", the matrix structure can have two columns (as described for <code>CTool_input_raw</code> ). If <code>NULL</code> , filled with zeros.
<code>Nin</code>	either matrix with a number of columns equal to the number of pools and a number of rows corresponding to simulation time steps (if <code>spinup</code> = <code>FALSE</code> ) or spin-up reference period (if <code>spinup</code> = <code>TRUE</code> ), in each case in accordance with number of rows of <code>Cin</code> , or list containing such matrices. If it is a list, each element of the list is expected to represent a stochastic repetition that covers input uncertainties. Then, the list must contain matrices of equal dimensions. Each matrix (or the one if modelling without uncertainties) must contain information about nitrogen input per pool and time step [ $\text{tN ha}^{-1}$ ]. When <code>CTool_input_raw</code> = <code>TRUE</code> , and <code>model</code> = "C-Tool" or <code>model</code> = "C-Tool-org" the matrix structure can have 2 columns (as described for <code>CTool_input_raw</code> ). If <code>NULL</code> , filled with zeros. Must contain entries $> 0$ where entries of <code>Cin</code> are $> 0$ . Only used when <code>calcN</code> = <code>TRUE</code> .

<code>Cin_wood</code>	list of lengths of different wood diameter classes. Each list element must be in <code>Cin</code> format and represent a specific wood diameter. Furthermore, the list elements themselves can be lists and contain stochastic repetitions, as explained for <code>Cin</code> . The mean diameter per class is defined in <code>wood_diam</code> . Only used when <code>model = "Yasso15"</code> or <code>model = "Yasso20"</code> .
<code>Nin_wood</code>	list of lengths of different wood diameter classes. Each list element must be in <code>Nin</code> format and represent a specific wood diameter. Furthermore, the list elements themselves can be lists and contain stochastic repetitions, as explained for <code>Nin</code> . The mean diameter per class is defined in <code>wood_diam</code> . Must contain entries of $> 0$ where entries of <code>Cin_wood</code> are $> 0$ . Only used when <code>calcN = TRUE</code> . Only used when <code>model = "Yasso15"</code> or <code>model = "Yasso20"</code> .
<code>wood_diam</code>	vector with wood diameter [cm]. The first element corresponds to the first list element of <code>Cin_wood</code> and <code>Nin_wood</code> . If <code>NULL</code> , filled with zeros. Only used when <code>Cin_wood</code> is specified and when either <code>model = "Yasso15"</code> or <code>model = "Yasso20"</code> . Must contain entries $\geq 0$ .
<code>xi</code>	either matrix with a number of columns equal to the number of pools and a number of rows corresponding to simulation time steps (if <code>spinup = FALSE</code> ) or spin-up reference period (if <code>spinup = TRUE</code> ), in each case in accordance with number of rows of <code>Cin</code> , or list containing such matrices. If it is a list, each element of the list is expected to represent a stochastic repetition that covers input uncertainties. Then, the list must contain matrices of equal dimensions. Each matrix (or the one if modelling without uncertainties) must contain information about time series of rate modifying factors for each model pool, built on the basis of annual decomposition rates. If <code>NULL</code> , filled with ones. Only used when <code>model</code> is <code>NULL</code> .

<code>env_in</code>	matrix with a model-specific number of columns and a number of rows corresponding to simulation time steps (if <code>spinup = FALSE</code> , and <code>tsteps = "weekly"</code> or <code>tsteps = "monthly"</code> ) or corresponding to simulation time steps multiplied by twelve (if <code>spinup = FALSE</code> and <code>tsteps = "annually"</code> or corresponding to individually chosen spin-up reference period (if <code>spinup = TRUE</code> ). The number of rows must be in accordance with the number of rows of <code>Cin</code> , except when <code>tsteps = "annually"</code> , then the number of rows must be twelve times the number of rows of <code>Cin</code> because monthly environmental variables still must be used to account for the annual cycle even when simulations run in annual mode. Contains environment-specific information to calculate rate modifying factors (instead of passing them with <code>xi</code> ) and initial carbon and nitrogen distributions (only RothC). When <code>model = "RothC"</code> , it must have four columns: atmospheric temperature (T) [°C], precipitation (p) [mm], evapotranspiration [mm] and a vector of zeros, ones (both originally RothC) or twos (not originally RothC) describing the soil cover, where ones indicate time steps when the soil is vegetated, zeros when it is bare and twos when it is bare, but this only influences the accumulated but not the maximum topsoil moisture deficit. The latter will then be calculated as if there was soil cover. The idea behind this is that the water content should be decisive for the microorganisms as a habitat and transport medium, regardless of whether a plant is growing or not. When <code>model = "Yasso07"</code> or <code>model = "Yasso15"</code> or <code>model = "Yasso20"</code> , it must have two columns: T [°C] and p [mm]. When <code>model = "C-Tool"</code> or <code>model = "C-Tool-org"</code> , it has one column: T [°C]. If <code>NULL</code> , filled with ones. Only used when <code>model</code> is not <code>NULL</code> .
<code>site</code>	vector of model-specific length. Contains site-specific information to calculate rate modifying factors (instead of passing them with <code>xi</code> ) and initial distributions. When <code>model = "RothC"</code> , it must be of length four: sample depth [mm], clay content [%], black sand status (0 or 1, 0 if unknown or if black sand method is not desired) and CN ratio (0 if unknown, but then either <code>C0</code> and <code>N0</code> must be passed or <code>calcC0 = TRUE</code> and <code>calcN0 = TRUE</code> , information on CN ratio given in <code>site</code> always takes precedence over internally calculated CN ratios). When <code>model = "C-Tool"</code> or <code>model = "C-Tool-org"</code> , it must be of length one: clay content [%]. Only used when <code>model = "RothC"</code> or <code>model = "C-Tool"</code> or <code>model = "C-Tool-org"</code> .
<code>theta</code>	either vector with model parameters for predefined models or matrix with rows of such parameters. If it is a matrix, each row is expected to represent a stochastic repetition that covers input uncertainties. If uncertainties are defined by another argument, e.g. <code>Cin</code> or <code>Nin</code> , these determine the number of stochastic repetitions and not <code>theta</code> . Then, if <code>theta</code> is a matrix, a parameter vector is randomly drawn for each uncertainty loop. Each vector (or row of matrix) must be of length 7 when <code>model = "RothC"</code> , of length 10 when <code>model = "C-Tool"</code> or <code>model = "C-Tool-org"</code> , of length 21 when <code>model = "Yasso07"</code> and of length 30 when <code>model = "Yasso15"</code> or <code>model = "Yasso20"</code> . If <code>NULL</code> , model-specific standard parameters are used instead. Only used when <code>model</code> is not <code>NULL</code> . See section 3.3 for details and standard parameters used.

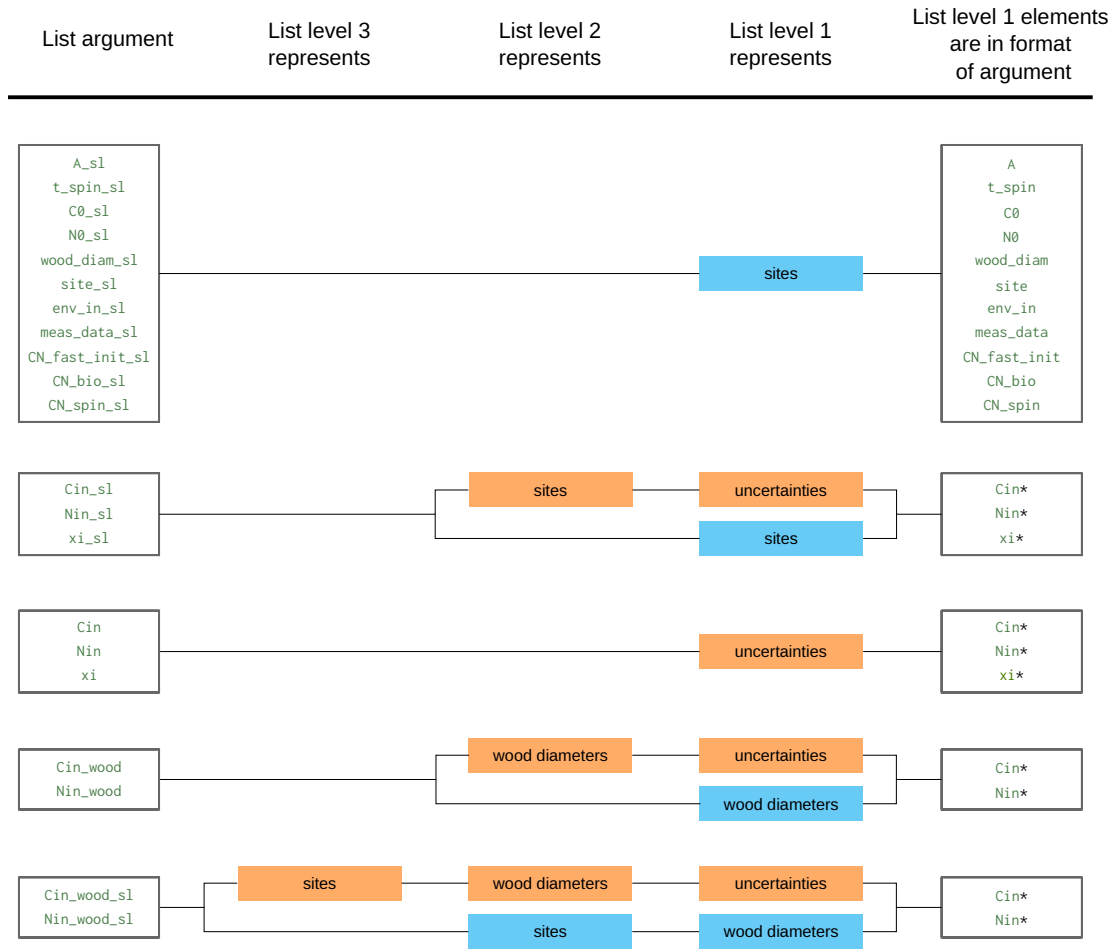
<code>theta_unc</code>	either number or vector of percentage values. If it is a vector, the same model-specific lengths as described for <code>theta</code> must be used. When used, model parameters modified by taking from the normal distribution around given values (either from <code>theta</code> or predefined values) with a standard deviation of <code>theta_unc</code> . This will be repeated as many times as defined in <code>theta_n_unc</code> or as defined by uncertainty dimensions of a carbon or nitrogen input argument (e.g. <code>Cin</code> ) and lead to unique model results and output list elements. Only used when <code>model</code> is not <code>NULL</code> and <code>theta</code> is not a matrix.
<code>theta_n_unc</code>	number of stochastic repetitions when model parameters for predefined models should be determined from a random distribution. Only used when the number of stochastic repetitions is not defined by another argument (e.g. <code>Cin</code> ). Only used when <code>model</code> is not <code>NULL</code> , <code>theta_unc</code> is not <code>NULL</code> and <code>theta</code> is not a matrix.
<code>meas_data</code>	matrix with a number of rows equal to the number of measurement points. The first column defines the time of measurement, the metric of which is based on simulation time steps. The second row must contain values of measured soil organic carbon stock. The third row must contain values of measured soil organic nitrogen and is only used when <code>calcN0 = TRUE</code> . Only used when <code>calcC0 = TRUE</code> .
<code>A_sl</code>	list with a length of number of sites to simulate. Each list element represents a site and must be in <code>A</code> format. Only used when <code>multisite = TRUE</code> and <code>model</code> is <code>NULL</code> . When <code>multisite = TRUE</code> , <code>A</code> can be passed instead of <code>A_sl</code> to have the same argument for all sites.
<code>C0_sl</code>	list with a length of number of sites to simulate. Each list element represents a site and must be in <code>C0</code> format. Only used when <code>multisite = TRUE</code> .
<code>N0_sl</code>	list with a length of number of sites to simulate. Each list element represents a site and must be in <code>N0</code> format. Only used when <code>multisite = TRUE</code> , <code>calcN = TRUE</code> and <code>calcN0 = FALSE</code> .
<code>Cin_sl</code>	list with a length of number of sites to simulate. Each list element represents a site and must be in <code>Cin</code> format, which can also contain uncertainties. Thus, <code>Cin_sl</code> can either be a list of different sites each containing lists of different uncertainty representations each with matrices of carbon input as described for <code>Cin</code> , or it can simply be a list of different sites each containing such matrices. Only used when <code>multisite = TRUE</code> .
<code>Nin_sl</code>	list with a length of number of sites to simulate. Each list element represents a site and must be in <code>Nin</code> format, which can also contain uncertainties. Thus, <code>Nin_sl</code> can either be a list of different sites each containing lists of different uncertainty representations each with matrices of carbon input as described for <code>Nin</code> , or it can simply be a list of different sites each containing such matrices. Only used when <code>multisite = TRUE</code> . Must contain entries $> 0$ where entries of <code>Cin_sl</code> are $> 0$ .

<code>Cin_wood_sl</code>	list with a length of number of sites to simulate. Each list element represents a site and must be in <code>Cin_wood</code> format, which can also contain uncertainties. Thus, <code>Cin_wood_sl</code> can either be a list of different sites each containing lists of different wood diameter representations, which in turn each contain lists of different uncertainty representations, each with matrices of carbon input as described for <code>Cin</code> , or it can simply be a list of different sites each containing lists of different wood diameter representations each containing such matrices. Only used when <code>multisite = TRUE</code> and either <code>model = "Yasso15"</code> or <code>model = "Yasso20"</code> .
<code>Nin_wood_sl</code>	list with a length of number of sites to simulate. Each list element represents a site and must be in <code>Nin_wood</code> format, which can also contain uncertainties. Thus, <code>Nin_wood_sl</code> can either be a list of different sites each containing lists of different wood diameter representations, which in turn each contain lists of different uncertainty representations, each with matrices of carbon input as described for <code>Nin</code> , or it can simply be a list of different sites each containing lists of different wood diameter representations each containing such matrices. Only used when <code>multisite = TRUE</code> and either <code>model = "Yasso15"</code> or <code>model = "Yasso20"</code> . Must contain entries $> 0$ where entries of <code>Cin_wood_sl</code> are $> 0$ .
<code>wood_diam_sl</code>	list with a length of number of sites to simulate. Each list element represents a site and must be in <code>wood_diam</code> format. Only used when <code>multisite = TRUE</code> and when either <code>model = "Yasso15"</code> or <code>model = "Yasso20"</code> .
<code>xi_sl</code>	list with a length of number of sites to simulate. Each list element represents a site and must be in <code>xi</code> format, which can also contain uncertainties. In the latter case, the site list must include uncertainty lists. Only used when <code>multisite = TRUE</code> and <code>model</code> is <code>NULL</code> .
<code>env_in_sl</code>	list with a length of number of sites to simulate. Each list element represents a site and must be in <code>env_in</code> format. Only used when <code>multisite = TRUE</code> .
<code>site_sl</code>	list with a length of number of sites to simulate. Each list element represents a site and must be in <code>site</code> format. Only used when <code>multisite = TRUE</code> .
<code>sitelist</code>	list with names of sites to simulate. Only used when <code>multisite = TRUE</code> .
<code>meas_data_sl</code>	list with a length of number of sites to simulate. Each list element represents a site and must be in <code>meas_data</code> format. Consequently, it is only used when <code>calcC0 = TRUE</code> and the third row of each list element is only used when <code>calcN0 = TRUE</code> . Only used when <code>multisite = TRUE</code> .
<code>calcN</code>	logical indicating whether soil organic nitrogen should be modeled.
<code>calcNbalance</code>	logical indicating whether the balance of nitrogen cycling should be calculated.
<code>calcN0</code>	logical indicating whether the initial amount of nitrogen should be calculated (instead of passing <code>N0</code> ). Then, the information in <code>meas_data</code> is used to determine initial states using linear regression.
<code>calcC0</code>	logical indicating whether the initial amount of carbon should be calculated (instead of passing <code>C0</code> ). Then, the information in <code>meas_data</code> is used to determine initial states using linear regression.

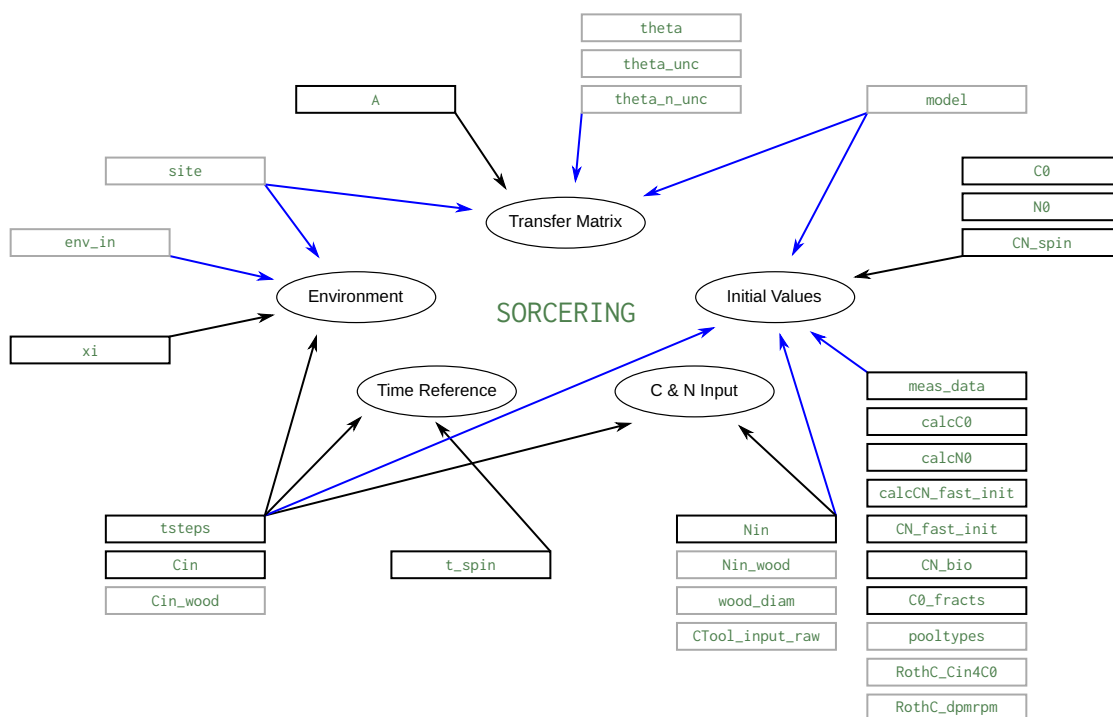


<code>calcCN_fast_init</code>	logical indicating whether to calculate the initial CN ratio for fast pools (using <code>Cin</code> and <code>Nin</code> ) or whether <code>CN_fast_init</code> should be used.
<code>CTool_input_raw</code>	logical defining of which type <code>Cin</code> and <code>Nin</code> are when modelling with <code>C-Tool</code> . If <code>TRUE</code> , <code>Cin</code> and <code>Nin</code> can only have two columns, one for the topsoil and one for the subsoil, and <code>SORCERING</code> is applying the <code>C-Tool</code> -specific distribution to model pools. If <code>FALSE</code> (default) <code>Cin</code> and <code>Nin</code> must have six columns, one per model pool. Only used when <code>model = "C-Tool"</code> or <code>model = "C-Tool-org"</code> .
<code>RothC_Cin4C0</code>	logical defining whether the SOC input should be used for the calculation of initial SOC. If <code>FALSE</code> the standard RothC ratio for agricultural soils of DPM to RPM of 0.59 to 0.41 or the ratio defined in <code>RothC_dpmrpm</code> is used. Only used when <code>model = "RothC"</code> .
<code>RothC_dpmrpm</code>	positive decimal number defining the initial ratio between DPM and RPM pool or vector containing such numbers. If vector, each element represents a site when <code>multisite = TRUE</code> . The predefined value of 1.439024 equals 0.59/0.41, the standard RothC ratio for agricultural soils. Only used when <code>model = "RothC"</code> .
<code>C0_fracts</code>	numerical vector of a length equal to the number of pools. Contains initial fractions of SOC in pools, the sum of which must be 1. Only used when <code>calcC0 = TRUE</code> or <code>C0</code> is a scalar.
<code>multisite</code>	logical indicating whether multiple sites should be calculated with one program call. Then, <code>t_spin</code> , <code>C0</code> , <code>N0</code> , <code>Cin</code> , <code>Nin</code> , <code>Cin_wood</code> , <code>Nin_wood</code> , <code>wood_diam</code> , <code>env_in</code> , <code>site_in</code> , <code>xi</code> and <code>meas_data</code> must be of list type and replaced with <code>t_spin_sl</code> , <code>C0_sl</code> , <code>N0_sl</code> , <code>Cin_sl</code> , <code>Nin_sl</code> , <code>Cin_wood_sl</code> , <code>Nin_wood_sl</code> , <code>wood_diam_sl</code> , <code>env_in_sl</code> , <code>site_in_sl</code> , <code>xi_sl</code> and <code>meas_data_sl</code> , respectively. <code>A</code> , <code>CN_bio</code> and <code>CN_fast_init</code> can be given as single variables or in list form of <code>A_sl</code> , <code>CN_bio_sl</code> and <code>CN_fast_init_sl</code> , respectively.
<code>pooltypes</code>	integer vector with a length equal to the number of pools. Contains information necessary for the calculation of <code>N0</code> . Allowed values are 1-6. 1: topsoil fast pool, 2: topsoil bio or humus pool, 3: topsoil chemically stable or inert pool, 4: subsoil fast pool, 5: subsoil bio or humus pool, 6: subsoil chemically stable or inert pool. Predefined values are (1,1,2,2,3) when <code>model = "RothC"</code> , (1,2,3,4,5,6) when <code>model = "C-Tool"</code> or <code>model = "C-Tool-org"</code> , (1,1,1,2,3) when <code>model = "Yasso07"</code> or <code>model = "Yasso15"</code> or <code>model = "Yasso20"</code> . Only used when <code>calcN = TRUE</code> and <code>calcN0 = TRUE</code> .
<code>CN_fast_init</code>	number that defines the initial CN ratio for fast pools ( <code>pooltypes = 1</code> or <code>4</code> ). Only used when <code>Nin</code> (or <code>Nin_sl</code> ) and <code>Cin</code> (or <code>Cin_sl</code> ) do not provide enough information for the estimation of initial nitrogen. The user will be informed about it when <code>init_info = TRUE</code> . Only used when <code>calcN = TRUE</code> and <code>calcN0 = TRUE</code> .
<code>CN_bio</code>	number that defines the initial CN ratio for slow pools ( <code>pooltypes = 2</code> or <code>5</code> ). Only used when <code>calcN = TRUE</code> and <code>calcN0 = TRUE</code> .

<code>CN_spin</code>	vector with a length equal to the number of pools. Defines the initial CN ratios for spin-up runs. For the case where the spinup starts from bare ground without soil organic components, the CN ratios of the pools must be defined. Since the CN ratios would then only be influenced by external inputs, the CN ratios for slow target pools without input would exceptionally be defined by the CN ratios of fast source pools due to a lack of alternatives. To prevent this, it is necessary to define initial CN ratios for spin-up runs in that case. Only used when <code>calcN = TRUE</code> and <code>spinup = TRUE</code> and for elements of which that of <code>C0</code> (and <code>N0</code> ) are zero.
<code>CN_fast_init_sl</code>	list with a length of number of sites to simulate. Each list element represents a site and must be in <code>CN_fast_init</code> format. Only used when <code>calcN = TRUE</code> , <code>multisite = TRUE</code> and <code>calcN0 = TRUE</code> . When <code>multisite = TRUE</code> , <code>CN_fast_init</code> can be passed instead of <code>CN_fast_init_sl</code> to have the same argument for all sites.
<code>CN_bio_sl</code>	list with a length of number of sites to simulate. Each list element represents a site and must be in <code>CN_bio</code> format. Only used when <code>calcN = TRUE</code> , <code>multisite = TRUE</code> and <code>calcN0 = TRUE</code> . When <code>multisite = TRUE</code> , <code>CN_bio</code> can be passed instead of <code>CN_bio_sl</code> to have the same argument for all sites.
<code>CN_spin_sl</code>	list of vectors that defines the initial CN ratios for spin-up runs. Each list element represents a site and must be in <code>CN_spin</code> format. Only used when <code>multisite = TRUE</code> , <code>calcN = TRUE</code> and <code>spinup = TRUE</code> and for elements of which that of <code>N0_sl</code> are zero. When <code>multisite = TRUE</code> , <code>CN_spin</code> can be passed instead of <code>CN_spin_sl</code> to have the same argument for all sites.
<code>init_info</code>	logical indicating whether additional information about the calculation of initial carbon, initial nitrogen, and CN ratio should be printed out during the simulations. Only used when <code>calcC0 = TRUE</code> or <code>calcN0 = TRUE</code> .
<code>model</code>	character string specifying a predefined soil organic carbon model to use. Valid options are "Yasso07", "Yasso15", "Yasso20", "RothC", "C-Tool" or "C-Tool-org". When not <code>NULL</code> , <code>xi</code> and <code>A</code> are calculated by <code>SORCERING</code> , and <code>env_in</code> must be specified. Additionally, <code>theta</code> can be specified to not use standard model parameters. (see section 3.3). If <code>calcN0 = TRUE</code> and <code>pooltypes = NULL</code> model-specific standard values for <code>pooltypes</code> are used.
<code>spinup</code>	logical indicating whether the simulations should run in spin-up mode. Then, from all time-depending input ( <code>Cin</code> , <code>Nin</code> , <code>xi</code> , <code>env_in</code> and site list derivatives) random years (consisting of one time step when <code>tsteps = "annually"</code> , of twelfth time steps when <code>tsteps = "monthly"</code> and of fifty-second time steps when <code>tsteps = "weekly"</code> ) are taken and <code>t_spin</code> defines the length of the spin-up. If modelling multiple sites, <code>t_spin_sl</code> allows for varying spin-up times. The length of the time-depending input is independent of the spin-up length.
<code>t_spin</code>	integer number of spin-up time steps.
<code>t_spin_sl</code>	list with a length of number of sites to simulate or integer number of spin-up time steps. If list, each list element represents a site and must be in <code>t_spin</code> format. If integer number, applied to all sites. Only used when <code>multisite = TRUE</code> .



**Figure 1:** List structure of **SORCERING** arguments. The arguments listed can either include uncertainties (orange structure path) or not (blue structure path). Arguments marked with an asterisk refer to those in matrix format.



**Figure 2:** Content structure of SORCERING arguments. Arguments with grey frames depend on using predefined models. Black arrows indicate direct definitions or direct influences. Blue arrows indicate indirect influences that are based on internal function calculations or definitions and can serve as an alternative to the direct definitions.

**Value**

`sorcering()` returns either a list of carbon and nitrogen output values or, when `multisite = TRUE`, a list broken down by site with result lists for each site. When uncertainties are modeled (as can be defined by passing e.g. `Cin`, `Nin`, `xi` or `theta`), the output is even extended to include another list dimension that covers these uncertainties. The lowest output list-level contains the following components:

<code>C</code>	matrix with a number of rows corresponding to simulation time steps (number of rows of <code>Cin</code> or number of rows of matrix elements in <code>Cin_sl</code> , when <code>spinup = FALSE</code> ), or to <code>t_spin</code> resp. <code>t_spin_sl</code> , when <code>spinup = TRUE</code> ) and a number of columns equal to the number of pools. Contains soil organic carbon [ $\text{tC ha}^{-1}$ ].
<code>N</code>	matrix with a number of rows corresponding to simulation time steps (number of rows of <code>Cin</code> or number of rows of matrix elements in <code>Cin_sl</code> , when <code>spinup = FALSE</code> ), or to <code>t_spin</code> resp. <code>t_spin_sl</code> , when <code>spinup = TRUE</code> ) and a number of columns equal to the number of pools. Contains soil organic nitrogen [ $\text{tN ha}^{-1}$ ]. Only generated when <code>calcN = TRUE</code> .
<code>Nloss</code>	matrix with a number of rows corresponding to simulation time steps (number of rows of <code>Cin</code> or number of rows of matrix elements in <code>Cin_sl</code> , when <code>spinup = FALSE</code> ), or to <code>t_spin</code> resp. <code>t_spin_sl</code> , when <code>spinup = TRUE</code> ) and a number of columns equal to the number of pools. Contains nitrogen losses [ $\text{tN ha}^{-1}$ ]. Positive values indicate that nitrogen was lost in the pools between this and the previous time steps (taking nitrogen decomposition and input into account). Only generated when <code>calcN = TRUE</code> .
<code>Nmin</code>	matrix with a number of rows corresponding to simulation time steps (number of rows of <code>Cin</code> or number of rows of matrix elements in <code>Cin_sl</code> , when <code>spinup = FALSE</code> ), or to <code>t_spin</code> resp. <code>t_spin_sl</code> , when <code>spinup = TRUE</code> ) and a number of columns equal to the number of pools. Contains nitrogen mineralisation [ $\text{tN ha}^{-1}$ ]. If values are negative, nitrogen immobilisation exceeds mineralisation. Only generated when <code>calcN = TRUE</code> .
<code>Nmin.sink.1,</code> <code>...,</code> <code>Nmin.sink.n</code>	matrices with a number of rows corresponding to simulation time steps (number of rows of <code>Cin</code> or number of rows of matrix elements in <code>Cin_sl</code> , when <code>spinup = FALSE</code> ), or to <code>t_spin</code> resp. <code>t_spin_sl</code> , when <code>spinup = TRUE</code> ) and a number of columns equal to the number of pools <code>n</code> . Contain pool-specific nitrogen mineralisation sinks [ $\text{tN ha}^{-1}$ ] (from the pool according to variable index [1, ..., n] to the pool according to column number). If the sink is the pool itself (index equals column number) the amount of decomposition is recorded. Only generated when <code>calcN = TRUE</code> .
<code>Nbalance</code>	matrix with a number of rows corresponding to simulation time steps (number of rows of <code>Cin</code> or number of rows of matrix elements in <code>Cin_sl</code> , when <code>spinup = FALSE</code> ), or to <code>t_spin</code> resp. <code>t_spin_sl</code> , when <code>spinup = TRUE</code> ) and three columns. Contains information on overall N changes in the soil between two time steps (first column) and information on total system N balance calculated based on total <code>Nloss</code> (second column) and based on total <code>Nmin</code> (third column) [ $\text{tN ha}^{-1}$ ]. Only generated when <code>calcN = TRUE</code> and <code>calcNbalance = TRUE</code> .

**Package Building Information**

The *SORCERING* code was written in C++ using the R packages *Rcpp* (Eddelbuettel et al. 2021a) and *RcppArmadillo* (Eddelbuettel et al. 2021b).

## Details

### 1 Introduction

**SORCERING** is a general model framework to describe soil organic carbon (SOC) dynamics and soil organic nitrogen (SON) dynamics based on models of first-order kinetics. It can be applied to any given SOC first-order kinetics model. The approach has already been successfully tested to describe SOC dynamics of Yasso (Tuomi et al. 2009, Viskari et al. 2020; 2022), RothC (Coleman and Jenkinson 1996) and C-Tool (Taghizadeh-Toosi et al. 2014). Moreover, it additionally offers the possibility of modelling N immobilisation and mineralisation by enhancing given SOC models by an additional N module. **SORCERING** was created using the C++ interface **Rcpp** (Eddelbuettel et al. 2021a) and can handle multiple sites and multiple stochastic representations with just one function call. This makes **SORCERING** a computationally efficient SOC and SON modelling tool.

In the following a description of each output value (see section 'Value') is given, details of the optional calculation of initial SOC and SON are presented, and predefined existing models and their functions are described.

## 2 Output Calculation

### 2.1 Value C

`SORCERING` calculates SOC applying a given SOC model for every simulation time step defined by passing `tsteps` and the number of rows of `Cin` (or number of rows of matrix elements in `Cin_sl`). SOC models applied here are defined by a number of pools, each characterised by specific decomposition and turnover rates. The underlying equation of first-order kinetics defines the change of SOC concentration in time as:

$$\frac{dC(t)}{dt} = Cin(t) + A_e(t) \cdot C(t) \quad (1)$$

The boundary condition  $Cin(t)$  and the initial condition  $C(0)$  must be defined beforehand (by passing `Cin` and `C0`, or by calculating with `SORCERING`-specific functions).  $A_e(t)$  is composed of transfer matrix  $A$  (as passed with `A` or provided by `model`) and the model-specific generated rate modifying factor series  $xi(t)$  (as passed with `xi` or calculated for a predefined `model`):

$$\begin{aligned} A_e(t) &= (A^T \cdot xi(t))^T \\ &= A \cdot diag(xi(t)) \end{aligned} \quad (2)$$

with superscript  $T$  denoting transposed matrices. Eq. 1 is valid for scalar values of  $A$ ,  $C$ ,  $xi$  and  $Cin$ , as well as for a square matrix  $A$  with side length of number of SOC pools  $n$  and related one dimensional vectors  $C$ ,  $xi$  and  $Cin$  with length  $n$ . Each element of  $C$ ,  $xi$  and  $Cin$  and each row and column of  $A$  thus stands for a specific pool. Off-diagonal elements of  $A$  describe SOC fluxes and diagonal elements describe SOC decomposition. Analytical solutions of eq. 1 are exponential functions and can be very complex with  $A$  containing many off-diagonals, i.e. SOC transfer between many pool pairs. Therefore, numerical solutions are an efficient way to solve the resulting complex equation system. In `SORCERING`, this equation system is solved by applying the fourth-order Runge-Kutta method:

$$C(t) = C(t-1) + \frac{1}{6}(K_1 + 2K_2 + 2K_3 + K_4) \quad (3)$$

with

$$\begin{aligned} K_1 &= Cin(t-1) + A \cdot diag(xi(t-1)) \cdot C(t-1) \\ K_2 &= Cin(t-1) + A \cdot diag\left(\frac{xi(t-1) + xi(t)}{2}\right) \cdot \left(C(t-1) + \frac{K_1}{2}\right) \\ K_3 &= Cin(t-1) + A \cdot diag\left(\frac{xi(t-1) + xi(t)}{2}\right) \cdot \left(C(t-1) + \frac{K_2}{2}\right) \\ K_4 &= Cin(t-1) + A \cdot diag(xi(t)) \cdot (C(t-1) + K_3) \end{aligned} \quad (4)$$

If negative values appear as a result of this numerical algorithm, the time step is successively reduced until no more negative values appear. Previously, this had only been necessary when `tsteps` = "annually".



## 2.2 Values $N$ and $N_{loss}$

As an extension to SOC modelling, **SORCERING** allows the modelling of SON coupled to the modelling of SOC. Its implementation is based on the following simplifying assumptions: (1) Nitrogen transfer and turnover rates are equal to carbon decomposition and transfer rates. (2) There is no N limitation in the soil, i.e. mineral N is always available for N immobilisation processes. (3) CN ratios of single pools are only affected by external inputs of C and N. The transfer of organic matter among pools does not affect CN ratios. As for SOC, the development of SON depends on boundary and initial conditions:  $N_{in}(t)$  and  $N(0)$  (passed with  $N_{in}$  and  $N0$ , or calculated with **SORCERING**-specific functions).

Given the input-considered SOC losses

$$C_{loss} = C(t-1) + C_{in}(t-1) - C(t) \quad (5)$$

and the input-considered NOC losses

$$N_{loss} = N(t-1) + N_{in}(t-1) - N(t) \quad (6)$$

between time points  $t$  and  $t-1$ , and assuming equal C and N decomposition rates

$$\frac{C_{loss}}{C(t)} = \frac{N_{loss}}{N(t)} \quad (7)$$

the amount of SON at each simulation time step is then calculated pool-wise as:

$$N(t) = \frac{N(t-1) + N_{in}(t-1)}{\left(\frac{C_{loss}}{C(t)} + 1\right)} \quad (8)$$

## 2.3 Values $N_{min}$ , $N_{min.sink}\langle 1 \rangle$ , ..., $N_{min.sink}\langle n \rangle$

Along with modelling SON, further quantities such as mineralisation rates are determined. In the following mineralisation is mentioned as if it includes mineralisation (positive values) and immobilisation (negative values). In contrast to nitrogen losses (eq. 6), mineralisation rates contain information about sources and sinks of SON. Pool-specific N mineralisation  $N_{min.sink}\langle j \rangle$  and N mineralisation  $N_{min}$  are related as follows:

$$N_{min_j}(t) = \sum_{p=1}^n N_{min.sink}\langle j \rangle_p(t) \quad (9)$$

for each simulation time point  $t$ , each pool  $j = 1, \dots, n$  and each pool  $p = 1, \dots, n$  and  $n$  total pools. Or in other words, the row sum of  $N_{min.sink}\langle j \rangle$  at one simulation time point equals the  $j^{\text{th}}$  column of  $N_{min}$  at that time point. Mineralisation rates and sinks are read from a mineralisation rates matrix  $N_{min.mat}$ :

$$N_{min_1}(t), \dots, N_{min_n}(t) = \sum_{i=1}^n N_{min.mat_{i,1}}(t), \dots, \sum_{i=1}^n N_{min.mat_{i,n}}(t) \quad (10)$$

$$Nmin.sink \langle j \rangle_1(t), \dots, Nmin.sink \langle j \rangle_n(t) = Nmin.mat_{j,1}(t), \dots, Nmin.mat_{j,n}(t) \quad (11)$$

and using the fourth-order Runge-Kutta Method  $Nmin.mat$  at time point  $t$  is calculated as follows:

$$Nmin.mat(t) = -\frac{1}{6}(Kn_1 + 2Kn_2 + 2Kn_3 + Kn_4) \quad (12)$$

with

$$\begin{aligned} Kn_1 &= (A \cdot diag(xi(t-1) \cdot C(t-1)))^T \cdot diag\left(\frac{1}{CN(t)}\right) \\ Kn_2 &= \left(A \cdot diag\left(\frac{xi(t-1) + xi(t)}{2} \cdot \left(C(t-1) + \frac{K_1}{2}\right)\right)\right)^T \cdot diag\left(\frac{1}{CN(t)}\right) \\ Kn_3 &= \left(A \cdot diag\left(\frac{xi(t-1) + xi(t)}{2} \cdot \left(C(t-1) + \frac{K_2}{2}\right)\right)\right)^T \cdot diag\left(\frac{1}{CN(t)}\right) \\ Kn_4 &= (A \cdot diag(xi(t) \cdot (C(t-1) + K_3)))^T \cdot diag\left(\frac{1}{CN(t)}\right) \end{aligned} \quad (13)$$

and superscript  $T$  denoting transposed matrices and

$$CN(t) = \begin{cases} \frac{C(t)}{N(t)}, & \forall N(t) > 0 \\ n.c., & \text{otherwise} \end{cases} \quad (14)$$

and  $K_1 - K_3$  taken from eq. system (4). Note that  $Kn_{1..4}$  are matrices and  $K_{1..3}$  are vectors.

As changes in SON must match the sums of all mineralisation paths, the sums over soil pools of **Nloss** and **Nmin**, respectively, must be approximately equal for all simulation time points:

$$\sum_{p=1}^n Nloss_p(t) \approx \sum_{p=1}^n Nmin_p(t) \quad (15)$$

A verification of this relation is given by **Nbalance** (see below).

## 2.4 Value **Nbalance**

The overall N change between two time steps is calculated as:

$$\Delta N(t) = \sum_{p=1}^n N_p(t-1) - \sum_{p=1}^n N_p(t) \quad (16)$$

The total system N balance serves as a verification output. Both of the following equations should always give results close to zero:

$$N_{bal1}(t) = \sum_{p=1}^n N_{in_p}(t-1) + \Delta N(t) - \sum_{p=1}^n N_{loss_p}(t) \approx 0 \quad (17)$$

$$N_{bal2}(t) = \sum_{p=1}^n Nin_p(t-1) + \Delta N(t) - \sum_{p=1}^n Nmin_p(t) \approx 0 \quad (18)$$

$\Delta N(t)$  is saved in the first column,  $N_{bal1}(t)$  in the second and  $N_{bal2}(t)$  in the third column of `Nbalance`.

### 3 Additional Features and Input Processing

#### 3.1 Estimation of Initial Soil Organic Carbon

If there is no initial SOC data, total initial SOC  $\Sigma C(0)_{est}$  can be estimated if there are more than two SOC measurement points (passed with `meas_data`) and the model is called with `calcC0 = TRUE`. Then,  $\Sigma C(0)_{est}$  is the intercept value (at the first time point) of the linear regression line through measured SOC data. In order to derive the initial SOC for each model pool, information about the initial SOC shares among pools  $C0_{fracts}$  is required. It can be passed with `C0_fracts` or, when a predefined SOC model is used, the model's standard fractions are taken (see section 3.3). The initial SOC distribution among the pools is then calculated with:

$$C(0)_{p=1}^n = \Sigma C(0)_{est} \cdot C0_{fracts,p} \quad (1)$$

with  $n$  being the number of SOC pools.

#### 3.2 Estimation of Initial Soil Organic Nitrogen

If there is no initial SON data, similarly to SOC, total initial SON  $\Sigma N(0)_{est}$  can be estimated if there are more than two SON measurement points (passed with `meas_data`) and the model is called with `calcCN0 = TRUE`. Likewise,  $\Sigma N(0)_{est}$  is the intercept value (at the first time point) of the linear regression line through measured SON data. To estimate the initial pool distribution of SON the model used must be classified into fast, slow and resistant pools (either via `pooltypes` or automatically when a predefined SOC model is used). Then, the initial SON in fast pools is calculated as:

$$N_{fast}(0) = \frac{C_{fast}(0)}{CN_{fast}(0)} \quad (2)$$

If `calcCN_fast_init = FALSE` (default), the initial CN ratio of fast pools  $CN_{fast}(0)$  is defined in `CN_fast_init` (40 by default). If `calcCN_fast_init = TRUE`,  $CN_{fast}(0)$  is estimated from organic inputs, or more specifically, it is thought to be typically the result of the direct input of organic C and N into these pools. Consequently, this method assumes that there has been similar management or natural input in the past, and the organic input during the simulation is used to estimate the initial CN ratio:

$$CN_{fast}(0) = \sum_{t=t_{in,first}}^{t_{in,last}} CN_{in}(t) \cdot weight(t) \quad (3)$$

However, not each input should have the same impact. Therefore, higher weights for early inputs and for higher amounts of inputs are used:

$$weight(t) = \frac{weight_t(t) \cdot weight_c(t)}{\sum_{T=t_{in,first}}^{t_{in,last}} (weight_t(T) \cdot weight_c(T))} \quad (4)$$

trivially with

$$\sum_{t=t_{in,first}}^{t_{in,last}} weight(t) = 1 \quad (5)$$

and with mass weight defined as:

$$weight_c(t) = \frac{C_{in}(t)}{\sum_{t=t_{in,first}}^{t_{in,last}} C_{in}(t)} \quad (6)$$

and temporal weight defined as:

$$weight_t(t) = \frac{1}{t^2} \quad (7)$$

If the sum of total carbon input during the simulation is smaller than the initial SOC, it is assumed that calculating the CN ratio from the inputs alone would lead to unrealistic results. As a solution, the missing amount of carbon is placed at the beginning of the  $C_{in}$  vector and `CN_fast_init` at the beginning of the CNfast vector for the calculations of equations 3 and 6. The user will be informed about those events when `init_info = TRUE`.

The initial amount of SON in slow and resistant pools  $N_{slow}(0)$  and  $N_{res}(0)$  are calculated as follows:

$$N_{slow}(0) = \frac{C_{slow}(0)}{CN_{slow}(0)} \quad (8)$$

$$N_{res}(0) = \frac{\Sigma C(0)}{\Sigma CN(0)_{est}} - (N_{fast}(0) + N_{slow}(0)) \quad (9)$$

with  $CN_{slow}$  initially starting with the given value of `CN_bio` (9 by default). If unrealistic values result out of the calculation, i.e.  $N_{res}(0) < 0$  or  $CN_{res}(0) = \frac{C_{res}(0)}{N_{res}(0)} > 100$ ,  $CN_{slow}(0)$  iteratively gets raised by 0.1 and eqs. 8 and 9 are iteratively repeated until realistic results are achieved. Assuming higher CN values in resistant pools than in slow pools, if  $CN_{res}(0)$  is smaller than  $CN_{slow}(0)$ ,  $CN_{slow}(0)$  iteratively gets lowered by 0.1 and eqs. 8 and 9 are iteratively repeated until  $CN_{res}(0)$  is not smaller than  $CN_{slow}(0)$ . Initial total CN ratio  $CN(0)$  is calculated as follows:

$$\Sigma CN(0)_{est} = \frac{\Sigma C(0)_{est}}{\Sigma N(0)_{est}} \quad (10)$$

and  $C_i(0)$  and  $N_i(0)$  being the intercept values by applying linear regressions through measured SOC and SON values, respectively. One should note that  $\Sigma C(0)$  may not be the same as  $\Sigma C(0)_{est}$  and therefore use the estimated SOC for the measured data-based calculation of  $N(0)$ .

### 3.3 Predefined Models

**SORCERING** can be run using existing predefined SOC models. The information about the transfer matrix and the rate modifying factors, which are formerly passed with **A** and **xi**, are then calculated based on environment-specific information **env\_in** (mandatory) and model parameters **theta** (when not passed, standard values will be used). At the moment one can choose among five models: Yasso07 (Tuomi et al. 2009), Yasso15 (Viskari et al. 2020), Yasso20 (Viskari et al. 2022), RothC (Coleman and Jenkinson 1996) or C-Tool (Taghizadeh-Toosi et al. 2014).

According to the definitions given in section 2.1, **A** is a matrix of size  $n \times n$  and  $xi(t)$  is a vector of length  $n$ , with  $n$  being the number of pools. For all predefined models  $n = 5$ , except for C-Tool, where  $n = 6$ .  $xi(t)$  vectors are calculated based on annual decomposition rates. Using the default value of **tsteps** = "monthly",  $xi(t)$  is divided by 12 and with **tsteps** = "weekly" by 52, which is not taken into account below. When **tsteps** = "annually",  $xi(t)$  is first calculated on a monthly base (that is why **env\_in** must also contain monthly values) and then the annual mean is used for the modelling. The **pooltypes** vector does not need to be passed with predefined models since default values are used. These values were created by the **SORCERING** developers out of logical considerations with the aim of SON initialization.

#### 3.3.1 Yasso

When modelling with Yasso, the user must pass either **model** = "Yasso07", **model** = "Yasso15" or **model** = "Yasso20" according to the three versions provided.

##### Parameters

When **model** = "Yasso07", a **theta** default vector of

$$\Theta_{Y07} = (kA, kW, kE, kN, kH, p_1 \dots p_{12}, pH, \beta_1, \beta_2, \gamma) \quad (11)$$

is used, and when **model** = "Yasso15" or **model** = "Yasso20", a **theta** default vector of

$$\Theta_{Y15} = \Theta_{Y20} = (kA, kW, kE, kN, kH, p_1 \dots p_{12}, pH, \beta_1, \beta_2, \beta_{N1}, \beta_{N2}, \beta_{H1}, \beta_{H2}, \gamma, \gamma_N, \gamma_H, \theta_1, \theta_2, r) \quad (12)$$

is used, with standard values listed in Table 1.

**Table 1:** Yasso standard parameters.

	Yasso07	Yasso15	Yasso20	
$kA$	0.66	0.49	0.51	Base decomposition rate for pool A [ $\text{yr}^{-1}$ ]
$kW$	4.3	4.9	5.19	Base decomposition rate for pool W [ $\text{yr}^{-1}$ ]
$kE$	0.35	0.24	0.13	Base decomposition rate for pool E [ $\text{yr}^{-1}$ ]
$kN$	0.22	0.095	0.1	Base decomposition rate for pool N [ $\text{yr}^{-1}$ ]
$kH$	0.0033	0.0013	0.0015	Base decomposition rate for pool H [ $\text{yr}^{-1}$ ]
$p_1$	0.32	0.44	0.5	Transference fraction from pool W to pool A
$p_2$	0.01	0.25	0	Transference fraction from pool E to pool A
$p_3$	0.93	0.92	1	Transference fraction from pool N to pool A
$p_4$	0.34	0.99	1	Transference fraction from pool A to pool W
$p_5$	0	0.084	0.99	Transference fraction from pool E to pool W
$p_6$	0	0.011	0	Transference fraction from pool N to pool W
$p_7$	0	0.00061	0	Transference fraction from pool A to pool E
$p_8$	0	0.00048	0	Transference fraction from pool W to pool E
$p_9$	0.01	0.066	0	Transference fraction from pool N to pool E
$p_{10}$	0	0.00077	0	Transference fraction from pool A to pool N
$p_{11}$	0	0.1	0.163	Transference fraction from pool W to pool N
$p_{12}$	0.02	0.65	0	Transference fraction from pool E to pool N
$pH$	0.04	0.0046	0.0015	Transference fraction from AWEN pools to pool H
$\beta_1$	0.076	0.091	0.158	First-order temperature parameter for AWE pools [ $^{\circ}\text{C}^{-1}$ ]
$\beta_2$	-0.00089	-0.00021	-0.002	Second-order temperature parameter for AWE pools [ $^{\circ}\text{C}^{-2}$ ]
$\beta_{N1}$	-	0.049	0.17	First-order temperature parameter for N pool [ $^{\circ}\text{C}^{-1}$ ]
$\beta_{N2}$	-	-0.000079	-0.005	Second-order temperature parameter for N pool [ $^{\circ}\text{C}^{-2}$ ]
$\beta_{H1}$	-	0.035	0.067	First-order temperature parameter for H pool [ $^{\circ}\text{C}^{-1}$ ]
$\beta_{H2}$	-	-0.00021	0	Second-order temperature parameter for H pool [ $^{\circ}\text{C}^{-2}$ ]
$\gamma$	-1.27	-1.8	-1.44	Precipitation impact parameter for AWE pools [ $\text{yr mm}^{-1}$ ]
$\gamma_N$	-	-1.2	-2	Precipitation impact parameter for N pool [ $\text{yr mm}^{-1}$ ]
$\gamma_H$	-	-13	-6.9	Precipitation impact parameter for H pool [ $\text{yr mm}^{-1}$ ]
$\theta_1$	-	-0.44	-2.55	First-order impact parameter for wood size [ $\text{cm}^{-1}$ ]
$\theta_2$	-	1.3	1.24	Second-order impact parameter for wood size [ $\text{cm}^{-2}$ ]
$r$	-	0.26	0.25	Exponent parameter for wood size

### Transfer Matrix

For all Yasso versions  $A$  looks like this:

$$A = \begin{pmatrix} -kA & p_1 & p_2 & p_3 & 0 \\ p_4 & -kW & p_5 & p_6 & 0 \\ p_7 & p_8 & -kE & p_9 & 0 \\ p_{10} & p_{11} & p_{12} & -kN & 0 \\ pH & pH & pH & pH & -kH \end{pmatrix} \quad (13)$$

### Environmental Factors

When `model = "Yasso07"`,  $xi(t)$  is calculated as follows:

$$\begin{aligned} xi_1(t) &= xi_2(t) = xi_3(t) = xi_4(t) = xi_5(t) \\ &= e^{\beta_1 T + \beta_2 T^2} (1 - e^{\gamma p}) \end{aligned} \quad (14)$$

When `model = "Yasso15"` or `model = "Yasso20"`,  $xi(t)$  is calculated as follows:

$$\begin{aligned} xi_1(t) &= xi_2(t) = xi_3(t) \\ &= e^{\beta_1 T(t) + \beta_2 T(t)^2} (1 - e^{\gamma p(t)}) \end{aligned} \quad (15)$$

$$xi_4(t) = e^{\beta_{N1} T(t) + \beta_{N2} T(t)^2} (1 - e^{\gamma_{Np} p(t)}) \quad (16)$$

$$xi_5(t) = e^{\beta_{H1} T(t) + \beta_{H2} T(t)^2} (1 - e^{\gamma_{Hp} p(t)}) \quad (17)$$

with  $T$  in degrees Celsius and  $p$  in mm, both passed with `env_in`.

### Initial Pool Properties

Initial pool properties described here apply equally to all three Yasso versions. When `calcN0 = TRUE`, a `pooltypes` default vector of (1, 1, 1, 2, 3) is used. When `calcC0 = TRUE` and `C0_fracts = Null`, a `C0_fracts` default vector of (0.15, 0.025, 0.025, 0.35, 0.45) is used, which could be a plausible initial carbon distribution for the Yasso pools. However, these values are not intended by the Yasso developers. It is recommended to perform model spinup runs for the initialisation of SOC.

### Input from Woody Litter

Woody litter is only considered when `model = "Yasso15"` or `model = "Yasso20"`. Then instead of `Cin` or `Cin_sl`, and instead of `Nin` or `Nin_sl`, `Cin_wood` or `Cin_wood_sl`, and `Nin_wood` or `Nin_wood_sl` must be passed. When `model = "Yasso15"` or `model = "Yasso20"`, by default an additional set of rate modifying factors  $xi_w(t)$  for each wood diameter class is calculated:



$$xi_w(t) = \min(1, (1 + \theta_1 \cdot diam + \theta_2 \cdot diam^2)^{-r}) \quad (18)$$

with  $\theta_1, \theta_2$  and  $r$  as described in section 3.3.1 and  $diam$  being the wood diameter as described in `wood_diam` or `wood_diam_sl`. Equation 2 then is exchanged with:

$$\begin{aligned} A_e(t) &= (A^T \cdot xi(t) \cdot xi_w(t))^T \\ &= A \cdot diag(xi(t) \cdot xi_w(t)) \end{aligned} \quad (19)$$

Since each wood diameter produces a new  $xi_w(t)$  the model calculation for each wood class is automatically run separately and after each time step the overall new SOC and SON are calculated as weighted means over all wood diameter input runs. The idea behind this separation of input diameter classes is that woody components are subject to delayed decomposition.

### 3.3.2 RothC

The RothC application used here uses standard RothC parameters and properties for agricultural soils (Coleman and Jenkinson 2014). This particularly affects the estimation of initial SOC. Therefore, especially if modelling non-agricultural soils, it is recommended to use the SOC input and pass `RothC_Cin4C0 = TRUE` to estimate the initial SOC.

#### Parameters

When `model = "RothC"`, a `theta` default vector of

$$\Theta_R = (k_{DPM}, k_{RPM}, k_{BIO}, k_{HUM}, k_{IOM}, R_{W,max}, R_{W,min}) \quad (20)$$

is used, with standard values listed in Table 2. Note that  $R_{W,max}$  and  $R_{W,min}$  are not typically intended by RothC developers to be modifiable parameters.

**Table 2:** RothC standard parameters.

$k_{DPM}$	10	Decomposition rate for DPM pool [ $\text{yr}^{-1}$ ]
$k_{RPM}$	0.3	Decomposition rate for RPM pool [ $\text{yr}^{-1}$ ]
$k_{BIO}$	0.66	Decomposition rate for BIO pool [ $\text{yr}^{-1}$ ]
$k_{HUM}$	0.02	Decomposition rate for HUM pool [ $\text{yr}^{-1}$ ]
$k_{IOM}$	0	Decomposition rate for IOM pool [ $\text{yr}^{-1}$ ]
$R_{W,max}$	1	Maximum rate modifying factor for soil moisture
$R_{W,min}$	0.2	Minimum rate modifying factor for soil moisture

### Transfer Matrix

A is build as follows:

$$A = \begin{pmatrix} -k_{DPM} & 0 & 0 & 0 & 0 \\ 0 & -k_{RPM} & 0 & 0 & 0 \\ B \cdot k_{DPM} & B \cdot k_{RPM} & B \cdot k_{BIO} - k_{BIO} & B \cdot k_{HUM} & 0 \\ H \cdot k_{DPM} & H \cdot k_{RPM} & H \cdot k_{BIO} & H \cdot k_{HUM} - k_{HUM} & 0 \\ 0 & 0 & 0 & 0 & -k_{IOM} \end{pmatrix} \quad (21)$$

with

$$B = \frac{0.46}{1 + 1.67(1.85 + 1.6e^{-0.0786 \cdot clay})} \quad (22)$$

$$H = \frac{0.54}{1 + 1.67(1.85 + 1.6e^{-0.0786 \cdot clay})} \quad (23)$$

and *clay* as defined in [site](#).

### Environmental Factors

$xi(t)$  is calculated as follows:

$$\begin{aligned} xi_1(t) &= xi_2(t) = xi_3(t) = xi_4(t) = xi_5(t) \\ &= R_T(t) \cdot R_C(t) \cdot R_W(t) \end{aligned} \quad (24)$$

with  $R_T(t)$  being the rate modifying factor series for temperature:

$$R_T(t) = \begin{cases} \frac{47.91}{1 + e^{\left(\frac{106.06}{T(t) + 18.27}\right)}}, & \forall T(t) > -18.27 \\ 0, & \text{otherwise} \end{cases} \quad (25)$$

and  $R_C(t)$  being the soil cover rate modifying factor:

$$R_C(t) = \begin{cases} 1, & \forall s_{cover}(t) = 0 \text{ or } s_{cover}(t) = 2 \\ 0.6, & \forall s_{cover}(t) = 1 \end{cases} \quad (26)$$

and  $R_W(t)$  being the topsoil moisture deficit (TSMD) rate modifying factor:

$$R_W(t) = \begin{cases} R_{W,max}, & \forall TSMD_{acc}(t) \geq 0.444 \cdot TSMD(t) \\ R_{W,min} + (R_{W,max} - R_{W,min}) \frac{TSMD_{max,pot} - TSMD_{acc}(t)}{TSMD_{max,pot} - 0.444 \cdot TSMD_{max,pot}}, & \text{otherwise} \end{cases} \quad (27)$$

and  $TSMD_{max,pot}(t)$  being the potentially, regardless of land cover, on the maximum remaining TSMD

$$TSMD_{max,pot}(t) = \begin{cases} TSMD_{max}(t)/1.8, & \forall s_{cover}(t) = 0 \\ TSMD_{max}(t), & \forall s_{cover}(t) = 1 \text{ or } s_{cover}(t) = 2 \end{cases} \quad (28)$$

and  $TSMD_{max}(t)$  being the maximum TSMD

$$TSMD_{max}(t) = -(20 + 1.3 \cdot clay - 0.01 \cdot clay^2) \frac{depth}{23} \quad (29)$$

and  $TSMD_{acc}(t)$  being the accumulated TSMD

$$TSMD_{acc}(t) = \begin{cases} \max(TSMD(t), WF(t)), & \forall WF(t) < 0 \text{ and } t = 0 \\ \max(TSMD(t), TSMD_{acc}(t-1) + WF(t)), & \forall TSMD_{acc}(t-1) + WF(t) < 0 \text{ and } t > 0 \\ 0, & \text{otherwise} \end{cases} \quad (30)$$

with

$$TSMD(t) = \begin{cases} TSMD_{max}(t)/1.8, & \forall s_{cover}(t) = 0 \text{ or } s_{cover}(t) = 2 \\ TSMD_{max}(t), & \forall s_{cover}(t) = 1 \end{cases} \quad (31)$$

and  $WF(t)$  describing the water flux

$$WF(t) = p(t) - ETP(t) \quad (32)$$

with  $clay$  and  $depth$  as defined in `site` and temperature  $T$ , precipitation  $p$ , evapotranspiration  $ETP$  and soil cover index  $s_{cover}$  as defined in `env_in`. Please note that  $TSMD_{max,pot}(t)$  only differs from  $TSMD(t)$  when  $s_{cover}(t) = 2$ .

### Initial Pool Properties

When `calcN0 = TRUE`, a `pooltypes` default vector of (1, 1, 2, 2, 3) is used. When `calcC0 = TRUE` and `C0_fracts = Null`, or `C0` is a scalar initial SOC fractions are calculated for the first four SOC pools, and the initial SOC of the fifth pool  $C(0)_{IOM}$  (inert pool IOM, as described by Falloon et al. 1998) is calculated directly out of the total  $C(0)$ :

$$C(0)_{IOM} = 0.049(C(0) - C0_{rel})^{1.139} + C0_{rel} \quad (33)$$

with  $C0_{rel}$  increasing the SOC in the inert pool of black sands based on a method of Springob and Kirchmann (2010):

$$C0_{rel} = \begin{cases} 0, & \forall CN(0) \leq 11 \vee bs_{flag} = 0 \\ \frac{C(0)(11-CN(0))}{CN(0)(\frac{11}{35}-1)}, & \forall CN(0) > 11 \wedge bs_{flag} = 1 \end{cases} \quad (34)$$

and  $bs_{flag}$  being the identifier of black sand soils as defined in `site`, and  $CN(0)$  being the CN ratio as defined in `site` or, if specified there by `entry = 0`, as calculated. In the latter case, the CN ratio is

calculated either as in eq. 10 or from  $C(0)$  and  $N(0)$ , depending on whether measured data should be used to estimate the initial CN ratio.

The initial state of the remaining carbon pools is calculated using a simplified version of the analytical solution from Dechow et al. (2019) assuming steady-state conditions. The initial SOC distribution among the five pools is then calculated as:

$$(C(0)_1, C(0)_2, C(0)_3, C(0)_4, C(0)_5) = (f_1 \cdot C(0), f_2 \cdot C(0), f_3 \cdot C(0), f_4 \cdot C(0), C(0)_{IOM}) \quad (35)$$

with

$$(f_1, f_2, f_3, f_4) = (f_{dpm}, f_{rpm}, f_{bio}, f_{hum}) \cdot \frac{C(0) - C(0)_{IOM}}{C(0)} \quad (36)$$

and

$$f_{dpm} + f_{rpm} + f_{bio} + f_{hum} = 1 \quad (37)$$

Following Dechow et al. (2019), these fractions are calculated as:

$$\begin{aligned} f_{dpm} &= \frac{fractI_1 \cdot k_{DPM}^{-1}}{fractI_1 \cdot u_{dpm} + fractI_2 \cdot u_{rpm}} \\ f_{rpm} &= \frac{fractI_2 \cdot k_{RPM}^{-1}}{fractI_1 \cdot u_{dpm} + fractI_2 \cdot u_{rpm}} \\ f_{bio} &= \frac{fractI_1 \cdot u_{bio,dpm} + fractI_2 \cdot u_{bio,rpm}}{fractI_1 \cdot u_{dpm} + fractI_2 \cdot u_{rpm}} \\ f_{hum} &= \frac{fractI_1 \cdot u_{hum,dpm} + fractI_2 \cdot u_{hum,rpm}}{fractI_1 \cdot u_{dpm} + fractI_2 \cdot u_{rpm}} \end{aligned} \quad (38)$$

with

$$fractI_1 = \begin{cases} dpmrpm, & \text{RothC\_Cin4C0} = \text{FALSE} \\ \frac{C_{in,tot,DPM}}{C_{in,tot,DPM} + C_{in,tot,RPM}}, & \text{RothC\_Cin4C0} = \text{TRUE} \end{cases} \quad (39)$$

and

$$fractI_2 = 1 - fractI_1 \quad (40)$$

and  $dpmrpm$  being the DPM to RPM ratio as defined in `RothC_dpmrpm` and  $C_{in,tot,DPM}$  and  $C_{in,tot,RPM}$  being the total SOC inputs (during the following simulation) into DPM and RPM pools, and

$$\begin{aligned} u_{dpm} &= k_{DPM}^{-1} + u_{bio,dpm} + u_{hum,dpm} \\ u_{rpm} &= k_{RPM}^{-1} + u_{bio,rpm} + u_{hum,rpm} \end{aligned} \quad (41)$$

and

$$u_{hum,dpm} = u_{hum,rpm} = \frac{1}{a_{1,2}} (-u_{bio,dpm}) \cdot a_{1,1} - \alpha_1 \quad (42)$$

and

$$u_{bio,dpm} = u_{bio,rpm} = \frac{\alpha_2 \cdot a_{1,2} - \alpha_1 \cdot a_{2,2}}{a_{1,1} \cdot a_{2,2} - a_{1,2} \cdot a_{2,1}} \quad (43)$$

and

$$\begin{aligned} a_{1,1} &= k_{BIO} \cdot (\alpha_1 - 1) \\ a_{1,2} &= k_{HUM} \cdot \alpha_1 \\ a_{2,1} &= k_{BIO} \cdot \alpha_2 \\ a_{2,2} &= k_{HUM} \cdot (\alpha_2 - 1) \end{aligned} \quad (44)$$

and

$$\begin{aligned} \alpha_1 &= cue \cdot 0.46 \\ \alpha_2 &= cue \cdot 0.54 \end{aligned} \quad (45)$$

and carbon use efficiency

$$cue = \frac{1}{1 + 1.67(1.85 + 1.6e^{-0.0786 \cdot clay})} \quad (46)$$

and *clay* being the clay content as defined in `site`.

### 3.3.3 C-Tool

C-Tool typically needs to be run twice, one time with `model = "C-Tool"` with `Cin` (and if desired `Nin`) of crop input and one time with `model = "C-Tool-org"` with `Cin` (and `Nin`) of organic input. In case of `model = "C-Tool-org"`, `C0` (and `N0`) should be zero. The user must calculate the overall C-Tool result independently as the sum of both runs. Thus, "C-Tool-org" is not a separate model, but rather a running mode of C-Tool.

## Parameters

When `model = "C-Tool"` or `model = "C-Tool-org"`, a `theta` default vector of

$$\Theta_C = (k_{FOMt}, k_{HUMt}, k_{ROMt}, k_{FOMs}, k_{HUMs}, k_{ROMs}, t_f, f_{CO_2}, f_{ROM}, f_{HUM}) \quad (47)$$

is used, with standard values taken from Taghizadeh-Toosi (2015) listed in Table 3.

**Table 3:** C-Tool standard parameters.

	C-Tool	C-Tool-org	
$k_{FOMt}$	1.44	1.44	Decomposition rate for FOM pool (topsoil) [ $\text{yr}^{-1}$ ]
$k_{HUMt}$	0.0336	0.0336	Decomposition rate for HUM pool (topsoil) [ $\text{yr}^{-1}$ ]
$k_{ROMt}$	0.000463	0	Decomposition rate for ROM pool (topsoil) [ $\text{yr}^{-1}$ ]
$k_{FOMs}$	1.44	1.44	Decomposition rate for FOM pool (subsoil) [ $\text{yr}^{-1}$ ]
$k_{HUMs}$	0.0336	0.0336	Decomposition rate for HUM pool (subsoil) [ $\text{yr}^{-1}$ ]
$k_{ROMs}$	0.000463	0	Decomposition rate for ROM pool (subsoil) [ $\text{yr}^{-1}$ ]
$t_f$	0.03	0	Fraction going to downward transport
$f_{CO_2}$	0.628	0.628	Fraction of $\text{CO}_2$ released
$f_{ROM}$	0.012	0	Fraction of fresh organic matter going to ROM pool
$f_{HUM}$	0	0.358	Fraction of input going to HUM pool

## Transfer Matrix

A is build as follows:

$$A = \begin{pmatrix} -k_{FOMt} & 0 & 0 & 0 & 0 & 0 \\ ai_{21} & -k_{HUMt} & 0 & 0 & 0 & 0 \\ 0 & ai_{32} & -k_{ROMt} & 0 & 0 & 0 \\ ai_{41} & 0 & 0 & -k_{FOMs} + ai_{44} & 0 & 0 \\ 0 & ai_{52} & 0 & ai_{54} & -k_{HUMs} + ai_{55} & 0 \\ 0 & 0 & ai_{63} & 0 & ai_{65} & -k_{ROMs} + ai_{66} \end{pmatrix} \quad (48)$$

with

$$\begin{aligned}
 ai_{21} &= (1 - t_f) \cdot h \cdot k_{FOMt} \\
 ai_{41} &= t_f \cdot k_{FOMt} \\
 ai_{32} &= f_{ROM} \cdot k_{HUMt} \\
 ai_{52} &= (1 - f_{CO_2} - f_{ROM}) \cdot k_{HUMt} \\
 ai_{63} &= (1 - f_{CO_2}) \cdot k_{ROMt} \\
 ai_{44} &= t_f \cdot k_{FOMs} \\
 ai_{54} &= (1 - t_f) \cdot h \cdot k_{FOMs} \\
 ai_{65} &= f_{ROM} \cdot k_{HUMs} \\
 ai_{55} &= (1 - f_{CO_2} - f_{ROM}) \cdot k_{HUMs} \\
 ai_{66} &= (1 - f_{CO_2}) \cdot k_{ROMs}
 \end{aligned} \tag{49}$$

and  $h$  being a factor that depends on clay content:

$$h = \frac{1}{1 + 1.67(1.85 + 1.6 \cdot e^{-7.86 \frac{clay}{100}})} \tag{50}$$

and  $clay$  being the clay content as defined in `site`.

### Input Transformation

If the input of SOC and SON is not defined for the single pools but only for topsoil and subsoil fractions (`CTool_input_raw = TRUE`) the standard way of distributing the fractions among the pools is used:

$$\begin{aligned}
 Cin(t) &= \\
 (Cin_{raw,top} \cdot (1 - F_{hum,clay}), Cin_{raw,top} \cdot F_{hum,clay}, 0, Cin_{raw,sub} \cdot (1 - F_{hum,clay}), Cin_{raw,sub} \cdot F_{hum,clay}, 0) \\
 Nin(t) &= \\
 (Nin_{raw,top} \cdot (1 - F_{hum,clay}), Nin_{raw,top} \cdot F_{hum,clay}, 0, Nin_{raw,sub} \cdot (1 - F_{hum,clay}), Nin_{raw,sub} \cdot F_{hum,clay}, 0)
 \end{aligned} \tag{51}$$

with

$$F_{hum,clay} = \max(0, f_{HUM} - h) \tag{52}$$

and  $f_{hum}$  and  $h$  as defined above, and with  $Cin_{raw,top}$  and  $Nin_{raw,top}$  being topsoil inputs and  $Cin_{raw,sub}$  and  $Nin_{raw,sub}$  being subsoil inputs.

### Environmental Factors

$xi(t)$  is calculated as follows:

$$\begin{aligned} xi_1(t) &= xi_2(t) = xi_3(t) = ft_t(t) \\ xi_4(t) &= xi_5(t) = xi_6(t) = ft_s(t) \end{aligned} \quad (53)$$

and

$$\begin{aligned} ft_t &= 7.24 \cdot e^{-3.432 + 0.168 T_{est,t}(t) \left(1 - \frac{T_{est,t}(t)}{73.8}\right)} \\ ft_s &= 7.24 \cdot e^{-3.432 + 0.168 T_{est,s}(t) \left(1 - \frac{T_{est,s}(t)}{73.8}\right)} \end{aligned} \quad (54)$$

and

$$\begin{aligned} T_{est,t} &= \bar{T} + amp \cdot e^{-\frac{d_t}{10 \cdot d_{damp}}} \cdot \sin(\rho \cdot (doy - offset)) \cdot 86400 - \frac{d_t}{10 \cdot d_{damp}} \\ T_{est,s} &= \bar{T} + amp \cdot e^{-\frac{d_s}{10 \cdot d_{damp}}} \cdot \sin(\rho \cdot (doy - offset)) \cdot 86400 - \frac{d_s}{10 \cdot d_{damp}} \end{aligned} \quad (55)$$

with  $\bar{T}$  being the average annual temperature,  $amp$  being the temperature range that lays between the 25% and the 75% quantile,  $d_t$  the number of the decimeter-wide soil layer that is relevant for the topsoil,  $d_s$  the one that is relevant for the subsoil (with standard values  $d_t = 2$  dm and  $d_s = 3$  dm), furthermore with  $d_{damp}$  being the damping depth,  $\rho$  being the angular frequency ( $= \pi \cdot 2/365/24/3600 = 1.992385 \cdot 10^{-7} \text{ sec}^{-1}$ ),  $doy$  being the day of the year and  $offset$  being defined as 110 days.  $\bar{T}$  is calculated using data from `tsteps` and `env_in`. Since  $amp$  is based on within-year fluctuations it is recommended to use a temporal resolution not coarser than a monthly one. Note that the function from `RcppArmadillo` (Eddelbuettel et al. 2021b) used to calculate the quantiles is equivalent to type 5 of the R `quantile` function.  $d_{damp}$  is calculated as follows:

$$d_{damp} = \sqrt{\frac{2Th_{diff}}{\rho}} = 1.874401 \text{ m} \quad (56)$$

with default thermal diffusivity of solid soil  $Th_{diff}$  of  $0.35 \cdot 10^{-6} \text{ m}^2 \text{ sec}^{-1}$ .

### Initial Pool Properties

When `calcN0 = TRUE`, a `pooltypes` default vector of (1,2,3,4,5,6) is used. When `calcC0 = TRUE` and `C0_fracts = Null`, a `C0_fracts` default vector of

$$\begin{aligned} C0_{fracts} &= (f_{FOMt}, f_{HUMt}, f_{ROMt}, f_{FOMs} \cdot sf, f_{HUMs} \cdot sf, f_{ROMs} \cdot sf) \\ &= (0.0316, 0.4804, 0.488, 0.003 \cdot sf, 0.3123 \cdot sf, 0.6847 \cdot sf) \\ &= (0.0316, 0.4804, 0.488, 0.00338298, 0.35216822, 0.77210880) \end{aligned} \quad (57)$$



is used, with  $f_{FOMt}$ ,  $f_{HUMt}$  and  $f_{ROMt}$  being the fresh organic, humus and resistant topsoil matter fractions, and  $f_{FOMt}$ ,  $f_{HUMt}$  and  $f_{ROMt}$  being those of the subsoil, and with  $sf$  being the subsoil factor defined as

$$sf = \frac{0.53}{0.47} = 1.12766 \quad (58)$$

Note that by default the first three pools in C-Tool represent the upper soil. Thus, to compare with other SOC models only the first three pools of the C-Tool output are relevant.

## Examples

```
#1 RothC application with fictional input for a single site

#1.1 Input

data(RothC_Cin_ex, RothC_Nin_ex, RothC_N0_ex, RothC_C0_ex, RothC_xi_ex,
     RothC_site_ex, RothC_env_in_ex) #fictional data

#1.2 Simulations

#In the following two methods are presented, one with a RothC as a predefined
#model (1.2.1), one where the RothC rate modifying factors must be calculated
#beforehand (1.2.2). Both methods lead to the same results.

#1.2.1 Simulation with predefined model

out_rothC <- sorcering( model="RothC", site=RothC_site_ex, env_in=RothC_env_in_ex,
                       Cin=RothC_Cin_ex, Nin=RothC_Nin_ex, N0=RothC_N0_ex, C0=RothC_C0_ex,
                       calcN=TRUE, tsteps="monthly")

#1.2.2 Simulation with own model definition and rate modifying factor definition

A_RothC <- fget_A_RothC(clay=30) #create transfer matrix for RothC
out_rothC_own <- sorcering(A=A_RothC, xi=RothC_xi_ex, Cin=RothC_Cin_ex,
                          Nin=RothC_Nin_ex, N0=RothC_N0_ex, C0=RothC_C0_ex, calcN=TRUE, tsteps="monthly")
#Note that RothC_xi_ex contains site and model specific rate modifying factors that
#are only valid in this specific example. Generally, xi must be calculated by the
#user for different environmental conditions and SOC models used.

#1.3 Results

#output structure summary
summary(out_rothC)

#show that results of 1.2.1 and 1.2.2 differ negligibly
all( abs(out_rothC$C-out_rothC_own$C) < 1e-14)
all( abs(out_rothC$N-out_rothC_own$N) < 1e-14)

#example plot
oldpar <- par(no.readonly=TRUE) #save old par
par(mfrow=c(1,1),mar=c(4,4,1,4))
plot(rowSums(out_rothC$N),axes=FALSE, col=1, cex.lab=2,xlab="",ylab="",ylim=c(0,9),
     pch=20)
par(new=TRUE)
plot(rowSums(RothC_Cin_ex)/rowSums(RothC_Nin_ex),
     axes=FALSE,col=2, cex.lab=2,xlab="",ylab="",ylim=c(0,60),pch=20)
axis(side=2, pos=0,
     labels=(0:6)*1.5, at=(0:6)*10, hadj=0.7, padj=0.5, cex.axis=2,las=1,col.axis=1)
axis(side=4, pos=60,
     labels=(0:6)*10, at=(0:6)*10, hadj=0, padj=0.5, cex.axis=2, las=1,col.axis=2)
axis(side=1, pos=0,
     labels= (0:6)*10, at=(0:6)*10, hadj=0.5, padj=0, cex.axis=2)
title(ylab=expression("total N [t ha^-1*"]"), line=2, cex.lab=2)
mtext("C input / N input", side=4, line=2, cex=2,col=2)
title(xlab="time", line=2, cex.lab=2)
par(oldpar) #back to old par
```

```

#2 RothC application with fictional input for a multiple site application

#2.1 Input

data(RothC_Cin_ex_sl, RothC_Nin_ex_sl, RothC_N0_ex, RothC_C0_ex, RothC_site_ex,
     RothC_env_in_ex) #fictional data

#2.2. Simulation

out_multi_rothC <- sorcering( model="RothC", site_sl=rep(list(RothC_site_ex),3),
                             env_in_sl=rep(list(RothC_env_in_ex),3), Cin_sl=RothC_Cin_ex_sl,
                             Nin_sl=RothC_Nin_ex_sl, N0_sl=rep(list(RothC_N0_ex),3),C0_sl=rep(list(RothC_C0_ex),3),
                             calcN=TRUE, tsteps="monthly", multisite=TRUE,
                             sitelist=list("normal","half_input","double_Cin"))

#2.3 Results

#output structure summary
summary(out_multi_rothC$normal)
summary(out_multi_rothC$half_input)
summary(out_multi_rothC$double_Cin)

#example plot
oldpar <- par(no.readonly=TRUE) #save old par
par(mfrow=c(1,1),mar=c(4,4,1,4))
for (listelement in c(1:3))
{
  lwidth<-1
  if (listelement==2)lwidth<-3
  plot(rowSums(out_multi_rothC[[listelement]]$N),axes=FALSE, col=1,type="l", lwd=lwidth,
       lty=listelement+2,cex.lab=2,xlab="",ylab="",ylim=c(0,18))
  par(new=TRUE)
  plot(rowSums(RothC_Cin_ex_sl[[listelement]])/rowSums(RothC_Nin_ex_sl[[listelement]]),
       type="l", lwd=lwidth, lty=listelement+2,axes=FALSE,col=2, cex.lab=2,xlab="",
       ylab="",ylim=c(0,120))
  par(new=TRUE)
}
axis(side=2, pos=0,
     labels=(0:6)*3, at=(0:6)*20, hadj=0.7, padj=0.5, cex.axis=2,las=1,col.axis=1)
axis(side=4, pos=60,
     labels=(0:6)*20, at=(0:6)*20, hadj=0, padj=0.5, cex.axis=2, las=1,col.axis=2)
axis(side=1, pos=0,
     labels= (0:6)*10 , at=(0:6)*10, hadj=0.5, padj=0, cex.axis=2)
title(ylab=expression("total N [t ha^-1*]"), line=2, cex.lab=2)
mtext("C input / N input", side=4, line=2, cex=2,col=2)
title(xlab="time", line=2, cex.lab=2)
legend(x=40,y=100,legend=c("normal","half_input","double_Cin"),lty=c(3,4,5),
      lwd=c(1,3,1))
par(oldpar) #back to old par

```

```

#3 RothC application with fictional input
#and fictional measurement data to calculate C0 and N0

#3.1 Input

#fictional data
data(RothC_Cin_ex_sl, RothC_Nin_ex_sl, RothC_site_ex, RothC_env_in_ex, meas_data_ex)

#3.2. Simulation

out_rothC_C0<-sorcering( model="RothC", site=RothC_site_ex, env_in=RothC_env_in_ex,
  Cin=RothC_Cin_ex, Nin=RothC_Nin_ex, calcC0=TRUE, calcN=TRUE, calcN0=TRUE,
  tsteps="monthly", meas_data=meas_data_ex)

#3.3 Results

#output structure summary
summary(out_rothC_C0)

#example plot
oldpar <- par(no.readonly=TRUE) #save old par
par(mfrow=c(1,1),mar=c(4,4,1,4))
plot(rowSums(out_rothC_C0$N),axes=FALSE, col=1, cex.lab=2,xlab="",ylab="",ylim=c(0,9),
  type="l",lwd=1)
par(new=TRUE)
plot(rowSums(out_rothC_C0$C),axes=FALSE, col=2, cex.lab=2,xlab="",ylab="",ylim=c(0,90),
  type="l",lwd=1)
par(new=TRUE)
plot(x=meas_data_ex[,1],y=meas_data_ex[,3],axes=FALSE, col=1, cex.lab=2,xlab="",ylab="",
  xlim=c(0,length(rowSums(out_rothC_C0$N))),ylim=c(0,9),pch=4,cex=3)
par(new=TRUE)
plot(x=meas_data_ex[,1],y=meas_data_ex[,2],axes=FALSE, col=2, cex.lab=2,xlab="",ylab="",
  xlim=c(0,length(rowSums(out_rothC_C0$N))),ylim=c(0,90),pch=4,cex=3)
par(new=TRUE)
axis(side=2, pos=0,
  labels=(0:8)*1, at=(0:8)*10, hadj=1, padj=0.5, cex.axis=2,las=1,col.axis=1)
axis(side=4, pos=60,
  labels=(0:8)*10, at=(0:8)*10, hadj=0, padj=0.5, cex.axis=2, las=1,col.axis=2)
axis(side=1, pos=0,
  labels= (0:8)*10 , at=(0:8)*10, hadj=0.5, padj=0, cex.axis=2)
title(ylab=expression("SON [t ha\"^-1*]"), line=2, cex.lab=2)
mtext(expression("SOC [t ha\"^-1*]"), side=4, line=3, cex=2,col=2)
title(xlab="time", line=2, cex.lab=2)
legend(x=30,y=30,legend=c("model result","measurement"),lwd=c(1,0))
legend(x=31,y=30,legend=c("", ""),pch=4,pt.cex=c(0,3),bty="n")
par(oldpar) #back to old par

```

```
#4 Yasso15 application using multiple sites and
#input values of different wood diameters which take uncertainties into account

#4.1 Input

data(Yasso_Cin_ex_wood_u_sl, Yasso_Nin_ex_wood_u_sl, Yasso_C0_ex_sl, Yasso_N0_ex_sl,
     RothC_env_in_ex) #fictional data

#show last entries of C input for 3rd site, 2nd wood layer, 4th uncertainty layer
tail(Yasso_Cin_ex_wood_u_sl[[3]][[2]][[4]])

#diameter of wood input: 2 classes of 0 cm and 10 cm for each of the 3 sites
wood_diam_ex_sl<-list(c(0,10),c(0,10),c(0,10))

#environmental variables
Yasso_env_in_ex<-RothC_env_in_ex[,1:2]

#4.2 Simulation

out_multi_yasso_wood_unc <- sorcering( model="Yasso15", C0_sl=Yasso_C0_ex_sl,
  env_in_sl=rep(list(Yasso_env_in_ex),3), wood_diam_sl=wood_diam_ex_sl,
  Cin_wood_sl=Yasso_Cin_ex_wood_u_sl,Nin_wood_sl=Yasso_Nin_ex_wood_u_sl,
  N0_sl=Yasso_N0_ex_sl, calcN=TRUE, tsteps="monthly", multisite=TRUE,
  sitelist=list("a","b","c"))

#4.3 Results

#show the last C results for 3rd site, 4th uncertainty layer
tail(out_multi_yasso_wood_unc[[3]][[4]]$C)
```

```

#5 RothC application using stochastically varying parameters
#and multiple sites

#5.1 fictional data
data(RothC_Cin_ex_sl, RothC_Nin_ex_sl, RothC_C0_ex, RothC_N0_ex,
     RothC_site_ex, RothC_env_in_ex)

#standard deviations [%] used for each of the 7 RothC theta parameters
RothC_theta_unc <- c(0,0,1,1,1,1,2)

#5.2 Simulation

out_sl <- sorcering( model="RothC", site_sl=rep(list(RothC_site_ex),3),
  env_in_sl=rep(list(RothC_env_in_ex),3), Cin_sl=RothC_Cin_ex_sl,
  Nin_sl=RothC_Nin_ex_sl, C0_sl=rep(list(RothC_C0_ex),3),
  N0_sl=rep(list(RothC_N0_ex),3), calcN=TRUE, theta_n_unc=10,
  theta_unc=RothC_theta_unc, multisite=TRUE,
  sitelist=list("normal","half_input","double_Cin"))

#5.3 Means and standard deviation

#60 time steps, 5 pools, 9 output types, 10 theta_n_unc, 3 sites
out_sl_arr <- array(unlist(out_sl),c(60,5,9,10,3))
out_sl_arr_N <- out_sl_arr[,2,,] #only output type 2: N
#mean over all uncerts
out_sl_arr_N_mean <- apply( out_sl_arr_N , c(1,2,4), na.rm=TRUE, FUN=mean )

#standard deviation
out_sl_arr_N_sd<-
array(0, dim=c(dim(out_sl_arr_N)[1],dim(out_sl_arr_N)[2],dim(out_sl_arr_N)[4]))
for (dim3 in c(1:dim(out_sl_arr_N)[4]))
  out_sl_arr_N_sd[, ,dim3]<-apply(out_sl_arr_N[, ,dim3],c(1:2),sd)

#5.4 Results

#show the last N means for stand 1
tail(out_sl_arr_N_mean[, ,1])

#show the last N standard deviations for stand 1
tail(out_sl_arr_N_sd[, ,1])

```

```
#6 How to create input lists for a RothC application using stochastically
#varying inputs and input scenarios
```

#### #6.1 Input

```
#fictional data
data(RothC_Cin_ex_sl, RothC_C0_ex, RothC_site_ex, RothC_env_in_ex)

#create input list of 3 scenarios, 100 uncertainties each
set.seed(17) #to make 'random' results reproducible
f1<-1
for (no in c(1:3)) #loop over 3 input scenarios
{
  #normal, half and double input
  Cin <- switch (no, RothC_Cin_ex, RothC_Cin_ex/2, RothC_Cin_ex*2)
  f2 <- 1
  #create fictional uncertainties
  for (unc in c(1:100)) #loop over 100 uncertainties
  {
    randnum<-max(0,rnorm(1,1,0.5)) #out of normal dist. with 50% sd.
    if (f2==1) Cin_u <- list(Cin*randnum) else
      Cin_u[[length(Cin_u)+1]] <- Cin*randnum
    f2 <- 0
  }
  if (f1==1) Cin_u_sl <- list(Cin_u) else
    Cin_u_sl[[length(Cin_u_sl)+1]] <- Cin_u
  f1 <- 0
}

#show input of scenario 3, uncertainty 51
head(Cin_u_sl[[3]][[51]])
```

#### #6.2 Simulation

```
out_sl <- sorcering( model="RothC", site_sl=rep(list(RothC_site_ex),3),
  env_in_sl=rep(list(RothC_env_in_ex),3),Cin_sl=Cin_u_sl,
  C0_sl=list(RothC_C0_ex,RothC_C0_ex,RothC_C0_ex), tsteps="monthly",
  multisite=TRUE, sitelist=list("normal","half_input","double_Cin"))
```

#### #6.3 Means and standard deviation

```
#60 time steps, 5 pools, 1000 uncertainties, 3 sites
out_sl_arr <- array(unlist(out_sl),c(60,5,100,3))

#means
out_sl_arr_mean <- apply( out_sl_arr , c(1,2,4), na.rm=TRUE, FUN=mean )

#standard deviation
out_sl_arr_sd<-
  array(0, dim=c(dim(out_sl_arr)[1],dim(out_sl_arr)[2],dim(out_sl_arr)[4]))
for (dim3 in c(1:dim(out_sl_arr)[4]))
  out_sl_arr_sd[, ,dim3]<-apply(out_sl_arr[, , ,dim3],c(1:2),sd)
```

## #6.4 Results

```

#C-pool sums of means for the 3 scenarios
totalC_m1<-rowSums(out_sl_arr_mean[,1])
totalC_m2<-rowSums(out_sl_arr_mean[,2])
totalC_m3<-rowSums(out_sl_arr_mean[,3])

#C-pool sums of standard deviations for the 3 scenarios
totalC_s1<-rowSums(out_sl_arr_sd[,1])
totalC_s2<-rowSums(out_sl_arr_sd[,2])
totalC_s3<-rowSums(out_sl_arr_sd[,3])

#example plot
oldpar <- par(no.readonly=TRUE) #save old par
par(mfrow=c(1,1),mar=c(4,4,1,4))
plot(totalC_m1,axes=FALSE, col=2, cex.lab=2,xlab="",ylab="",ylim=c(0,100),
     type="l",lwd=1)
par(new=TRUE)
plot(totalC_m2,axes=FALSE, col=3, cex.lab=2,xlab="",ylab="",ylim=c(0,100),
     type="l",lwd=1)
par(new=TRUE)
plot(totalC_m3,axes=FALSE, col=4, cex.lab=2,xlab="",ylab="",ylim=c(0,100),
     type="l",lwd=1)
par(new=TRUE)
polygon(c(1:60,60:1),c(totalC_m1+totalC_s1, rev(totalC_m1-totalC_s1)),
       border=NA,col=rgb(1,0,0,0.27),density=40,angle=180,xlab="",ylab="")
par(new=TRUE)
polygon(c(1:60,60:1),c(totalC_m2+totalC_s2, rev(totalC_m2-totalC_s2)),
       border=NA,col=rgb(0,1,0,0.27),density=30,xlab="",ylab="")
par(new=TRUE)
polygon(c(1:60,60:1),c(totalC_m3+totalC_s3, rev(totalC_m3-totalC_s3)),
       border=NA,col=rgb(0,0,1,0.27),density=25,angle=90,xlab="",ylab="")
par(new=TRUE)
axis(side=2, pos=0,
     labels=(0:10)*1, at=(0:10)*10, hadj=1, padj=0.5, cex.axis=2,las=1,col.axis=1)
axis(side=1, pos=0,
     labels= (0:6)*10 , at=(0:6)*10, hadj=0.5, padj=0, cex.axis=2)
title(ylab=expression("SOC [t ha^{-1}]"), line=2, cex.lab=2)
title(xlab="time", line=2, cex.lab=2)
legend(x=20,y=30,fill=c(0,0,0,4,2,3),density=c(0,0,0,25,40,30),angle=c(0,0,0,90,0,45),
      border=c(0,0,0,1,1,1),legend=c("mean double input scenario",
      "mean regular input scenario", "mean half input scenario",
      "uncertainty range double input scenario", "uncertainty range regular input scenario",
      "uncertainty range half input scenario"))
legend(x=20,y=30,lty=c(1,1,1,0,0,0),seg.len=c(1,1,1,0,0,0), col=c(4,2,3,0,0,0),
      legend=c("","","","","",""),bty="n")
par(oldpar) #back to old par

```



```

#7 RothC application with fictional input for a spin-up application

#7.1 Input

#fictional data
data(RothC_Cin_ex_sl_spin, RothC_Nin_ex_sl_spin, RothC_site_ex, RothC_env_in_ex)

#7.2. Simulation

out_multi_rothC <- sorcering( model="RothC", site_sl=rep(list(RothC_site_ex),3),
  env_in_sl=rep(list(RothC_env_in_ex[1:12,]),3), Cin_sl=RothC_Cin_ex_sl_spin,
  Nin_sl=RothC_Nin_ex_sl_spin, calcN=TRUE, tsteps="monthly", multisite=TRUE,
  sitelist=list("normal","half_input","double_Cin"), spinup=TRUE, t_spin_sl=36000,
  C0=c(0,0,0,0,20), N0=c(0,0,0,0,2), CN_spin=c(100,100,50,50,10))

#7.3 Results

#example plot
oldpar <- par(no.readonly=TRUE) #save old par
par(mfrow=c(1,1),mar=c(4,4,1,4))
for (listelement in c(1:3))
{
  lwidth<-1
  if (listelement==2)lwidth<-3
  printN<-rowSums(out_multi_rothC[[listelement]]$N)
  printseq<-seq.int(1L,length(printN),100L)
  printC<-rowSums(out_multi_rothC[[listelement]]$C)
  plot(printN[printseq],axes=FALSE, col=1,type="l", lwd=lwidth,
    lty=listelement+2,cex.lab=2,xlab="",ylab="",ylim=c(0,30))
  par(new=TRUE)
  plot(printC[printseq],axes=FALSE, col=2,type="l", lwd=lwidth,
    lty=listelement+2,cex.lab=2,xlab="",ylab="",ylim=c(0,180))
  par(new=TRUE)
}
axis(side=2, pos=0,
  labels=(0:6)*5, at=(0:6)*30, hadj=0.7, padj=0.5, cex.axis=2,las=1,col.axis=1)
axis(side=4, pos=360,
  labels=(0:6)*30, at=(0:6)*30, hadj=0, padj=0.5, cex.axis=2, las=1,col.axis=2)
axis(side=1, pos=0,
  labels= (0:6)*6000 , at=(0:6)*60, hadj=0.5, padj=0, cex.axis=2)
title(ylab=expression("total N [t ha-1"]"), line=2, cex.lab=2)
mtext(expression("total C [t ha-1"]"), side=4, line=2, cex=2,col=2)
title(xlab="time", line=2, cex.lab=2)
legend(x=120,y=140,legend=c("normal","half_input","double_Cin"),lty=c(3,4,5),
  lwd=c(1,3,1))
par(oldpar) #back to old par

```

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