

Package ‘ider’

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Title Various Methods for Estimating Intrinsic Dimension

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Description An implementation of various methods for estimating intrinsic dimension of vector-valued dataset or distance matrix. Most methods implemented are based on different notion of fractal dimension such as the capacity dimension, the box-counting dimension, and the information dimension.

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Imports FNN, stats, glm2

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Description

This package is used for estimating intrinsic dimension of a given dataset.

Details

In common data analysis situations, an observed datum is expressed by a p -dimensional vector. In general, the apparent data dimension p and its intrinsic dimension d are different. A basic assumption in many data analysis and machine learning methods is that the intrinsic dimension is low even when the apparent dimension is high and the data distribution is constrained onto a low dimensional manifold. Examples of such methods include manifold learning, subspace methods, and visualization and dimensionality reduction methods. The key to the success of dimensionality reduction, manifold learning and latent variable analysis lies in the accurate estimation of the intrinsic dimension of the dataset at hand. This package implements a number of intrinsic dimension estimation methods. Some functions are for estimating the global intrinsic dimension while others are capable of estimating both local and global intrinsic dimension.

The package has functions `corint`, `convU`, `lbmle`, `nni`, `pack` for estimating global intrinsic dimensions, and `mada`, `side` for estimating local intrinsic dimensions. A data generator `gendata` is included in the package.

Author(s)

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References

- P. Grassberger and I. Procaccia. Measuring the strangeness of strange attractors. *Physica*, 1983.
- E. Levina and P. J. Bickel. Maximum likelihood estimation of intrinsic dimension. *Advances in Neural Information Processing Systems* 17, 2005.
- D. MacKay and Z. Ghahramani. <http://www.inference.org.uk/mackay/dimension/>
- K. W. Pettis et al. An intrinsic dimensionality estimator from near neighbor information. *IEEE transactions on pattern recognition and machine intelligence*, 1979.
- M. Hein and J-Y. Audibert. Intrinsic dimensionality estimation of submanifolds in \mathbb{R}^d . *International Conference on Machine Learning*, 2005.
- B. Kegl. Intrinsic dimension estimation using packing numbers. *Advances in Neural Information Processing Systems* 15, 2002.
- B. Eriksson and M. Crovella. Estimating intrinsic dimension via clustering. *IEEE Statistical Signal Processing Workshop*, 2012.
- H. Hino, J. Fujiki, S. Akaho, and N. Murata, 'Local Intrinsic Dimension Estimation by Generalized Linear Modeling', *Neural Computation*, 2017

Examples

```

## Not run:
## global intrinsic dimension estimate
x <- gendata(DataName='SwissRoll',n=300)

x <- gendata(DataName='SwissRoll',n=300,p=3,q=2)
estcorint <- corint(x=x,k1=5,k2=10)
print(estcorint)

estmle <- lbmle(x=x,k1=3,k2=5) ## estimation by mle
print(estmle)

estnii <- nni(x=x) ## estimation by nearest neighbor information
print(estnii)

estconvU <- convU(x=x) ## estimation by convergence property of U-stats
print(estconvU)

estpackG <- pack(x=x,greedy=TRUE) ## estimation by the packing number method with greedy algorithm
print(estpackG)
estpackC <- pack(x=x,greedy=FALSE) ## estimation by the packing number method by clustering
print(estpackC)

## local intrinsic dimension estimate
tmp <- gendata(DataName='ldbl',n=300)
x <- tmp$x
estmada <- mada(x=x,local=TRUE)
head(estmada) ## estimated local intrinsic dimensions by mada
head(tmp$tDim) ## true local intrinsic dimensions
estside <- side(x=x,local=TRUE)
head(estside) ## estimated local intrinsic dimensions by side

## End(Not run)

```

convU

Intrinsic Dimension Estimation with Convergence Property of a U-statistics.

Description

convU estimates intrinsic dimension of given dataset based on the convergence property of Ustatistics(smoothed correlation dimension) w.r.t. kernel bandwidth

Usage

```
convU(x, maxDim = 5, DM = FALSE)
```

Arguments

x	data matrix or distance matrix given by <code>as.matrix(dist(x))</code> .
maxDim	maximum of the candidate dimension.
DM	whether 'x' is distance matrix or not. logical.

Details

A variant of fractal dimension called the correlation dimension is considered. The correlation dimension is defined by the notion of the correlation integral, which is calculated by counting the number of pairs closer than certain threshold epsilon. The counting operation is replaced with the kernel smoothed version, and based on the convergence property of the resulting U-statistics, an intrinsic dimension estimator is derived.

Value

Estimated global intrinsic dimension.

Author(s)

Hideitsu Hino <hideitsu.hino@gmail.com>

References

M. Hein and J-Y. Audibert. Intrinsic dimensionality estimation of submanifolds in R^d . International Conference on Machine Learning, 2005.

Examples

```
x <- gendata(DataName='SwissRoll',n=300)
estconvU <- convU(x=x)
print(estconvU)
```

corint

Intrinsic Dimension Estimation with Correlation Integral

Description

corint estimates intrinsic dimension of given dataset based on the correlation integral

Usage

```
corint(x, k1 = NULL, k2 = NULL, DM = FALSE, p = NULL)
```

Arguments

x	data matrix or distance matrix given by <code>as.matrix(dist(x))</code> .
k1	first k-NN parameter.
k2	second k-NN parameter.
DM	whether 'x' is distance matrix or not. logical.
p	ambient dimension used for automatically define 'k1' and 'k2'.

Details

A variant of fractal dimension called the correlation dimension is considered. The correlation dimension is defined by the notion of the correlation integral, is calculated by using the power law for the definition of the correlation dimension.

Value

Estimated global intrinsic dimension.

Author(s)

Hideitsu Hino <hideitsu.hino@gmail.com>

References

P. Grassberger and I. Procaccia. Measuring the strangeness of strange attractors. *Physica*, 1983.

Examples

```
x <- gendata(DataName='SwissRoll',n=300)
estcorint <- corint(x=x,k1=5,k2=10)
print(estcorint)
```

gendata

Data generator for intrinsic dimension estimation.

Description

gendata generates various artificial datasets for intrinsic dimension estimation experiments.

Usage

```
gendata(  
  DataName = "SwissRoll",  
  n = 300,  
  p = NULL,  
  noise = NULL,  
  ol = NULL,
```

```

    curv = 1,
    seed = 123,
    sorted = FALSE
  )

```

Arguments

DataName	Name of dataset, one of the following: <ul style="list-style-type: none"> • SwissRoll: SwissRoll data, 2D manifold in 3D space. • NDSwissRoll: Non-deformable SwissRoll data, 2D manifold in 3D space. • Moebius: Moebius strip, 2D manifold in 3D space. • SphericalShell: Spherical Shell, (p-1)-dimensional manifold in p-dimensional space. • Sinusoidal: Sinusoidal data, 1D manifold in 3D space. • Spiral: Spiral-shaped 1D manifold in 2D space. • Cylinder: Cylinder-shaped 2D manifold in 3D space. • SShape: S-shaped 2D manifold in 3D space. • ldbl: LDB(line - disc - filled ball - line), embedded in 3D space (original dataset).
n	number of data points to be generated.
p	ambient dimension of the dataset.
noise	parameter to control noise level in the dataset. In many cases, it is used for sd of rnorm used inside the function.
ol	percentage of outliers, i.e., n * ol outliers are added to the generated dataset.
curv	a parameter to control the complexity of the embedded manifold.
seed	random number seed.
sorted	logical. If TRUE, the index of the generated dataset is sorted with respect to x-axis for the ease of visualization.

Details

This function generates various artificial datasets often used in manifold learning and dimension estimation researches. For some datasets, complexity of the shape is controlled by the parameter `curv`. The parameters `noise` and `outlier` are used for adding noise and/or outliers for the dataset.

Value

Data matrix. For `ldbl` dataset, it outputs a list composed of `x`: data matrix and `tDim`: true intrinsic dimension for each point.

Author(s)

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Examples

```
## global intrinsic dimension estimate
x <- gendata(DataName='SwissRoll')
estmle <- lbmle(x=x,k1=3,k2=5)
print(estmle)

## local intrinsic dimension estimate
tmp <- gendata(DataName='ldbl',n=1000)
x <- tmp$x
estmada <- mada(x=x,local=TRUE)
head(estmada) ## estimated local intrinsic dimensions
head(tmp$tDim) ## true local intrinsic dimensions
```

handD

Hand rotation data

Description

Data from a QTL experiment on gravitropism in Arabidopsis, with data on 162 recombinant inbred lines (Ler x Cvi). The outcome is the root tip angle (in degrees) at two-minute increments over eight hours.

Usage

```
data(handD)
```

Format

An object of class 'dist'.

References

E. Levina and P. J. Bickel. Maximum likelihood estimation of intrinsic dimension. *Advances in Neural Information Processing Systems* 17, 2005.

B. Kegl. Intrinsic dimension estimation using packing numbers. *Advances in Neural Information Processing Systems* 15, 2002.

H. Hino, J. Fujiki, S. Akaho, and N. Murata, 'Local Intrinsic Dimension Estimation by Generalized Linear Modeling', *Neural Computation*, 2017

Examples

```
data(handD)
estmle <- lbmle(x=handD,DM=TRUE,k1=5,k2=10)
print(estmle)
```

`lbmle`*Maximum Likelihood Estimation of Intrinsic Dimension.*

Description

`lbmle` estimate the intrinsic dimension of a given dataset.

Usage

```
lbmle(x = NULL, k1 = NULL, k2 = NULL, BC = TRUE, DM = FALSE, p = NULL)
```

Arguments

<code>x</code>	data matrix or distance matrix given by <code>as.matrix(dist(x))</code> .
<code>k1</code>	first k-NN parameter.
<code>k2</code>	second k-NN parameter.
<code>BC</code>	whether bias is corrected or not. logical.
<code>DM</code>	whether 'x' is distance matrix or not. logical.
<code>p</code>	ambient dimension used for automatically define 'k1' and 'k2'.

Details

The likelihood of the rate parameter of the Poisson process, which characterize the behaviour of the distance from a point to another point in the given dataset, is considered, and the maximum likelihood estimator (MLE) for the intrinsic dimension is derived. The original method proposed by Levina and Bickel contains a known bias, and it is corrected by Mackay and Ghahramani. This function implements both, with the default the bias corrected estimate.

Value

Estimated global intrinsic dimension.

Author(s)

Hideitsu Hino <hideitsu.hino@gmail.com>

References

E. Levina and P. J. Bickel. Maximum likelihood estimation of intrinsic dimension. *Advances in Neural Information Processing Systems* 17, 2005.

D. MacKay and Z. Ghahramani. <http://www.inference.org.uk/mackay/dimension/>

Examples

```
x <- gendata(DataName='SwissRoll',n=300)
estmle <- lbmle(x=x,k1=3,k2=5)
print(estmle)
```

mada

Manifold-Adaptive Local Dimension Estimation.

Description

mada estimates local information dimension of given dataset based on the first order expansion of probability mass function.

Usage

```
mada(x, k = NULL, comb = "average", DM = FALSE, local = FALSE, maxDim = 5)
```

Arguments

x	data matrix or distance matrix given by <code>as.matrix(dist(x))</code> .
k	k-NN parameter.
comb	'average', 'median' or 'vote' for combining local estimates when global estimate is required.
DM	whether 'x' is distance matrix or not. logical.
local	logical. If TRUE, a vector of local dimensions at each sample point is returned.
maxDim	maximum of the candidate dimensions.

Details

A variant of fractal dimension called the local information dimension is considered. The local information dimension is estimated by using the probability mass function. The function `mada` considers first order expansion of the probability mass around the inspection point, and it estimates the local information dimension by using two different radii from the inspection point.

Value

Estimated local or global intrinsic dimension.

Author(s)

Hideitsu Hino <hideitsu.hino@gmail.com>

References

A. M. Farahmand, C. Szepesvari and J-Y. Audibert. Manifold-adaptive dimension estimation. International Conference on Machine Learning, 2007.

Examples

```
## local intrinsic dimension estimate
tmp <- gendata(DataName='ldbl',n=300)
x <- tmp$x
estmada <- mada(x=x,local=TRUE)
head(estmada) ## estimated local intrinsic dimensions by mada
head(tmp$tDim) ## true local intrinsic dimensions
```

nni

*Intrinsic Dimensionality Estimation from Near-Neighbor Information.***Description**

nni estimates intrinsic dimension of given dataset based on the nearest-neighbor information.

Usage

```
nni(x, k1 = 2, k2 = 30, DM = FALSE, eps = 0.01, p = NULL)
```

Arguments

x	data matrix or distance matrix given by <code>as.matrix(dist(x))</code> .
k1	first k-NN parameter.
k2	second k-NN parameter.
DM	whether 'x' is distance matrix or not. logical.
eps	accuracy parameter.
p	ambient dimension used for automatically define 'k1' and 'k2'.

Details

First order expansion of the probability mass function is considered, then the distribution of the nearest-neighbor points from the inspection point is modeled by the Poisson distribution. The average of the nearest-distance is expressed by intrinsic dimension to be estimated.

Value

Estimated global intrinsic dimension.

Author(s)

Hideitsu Hino <hideitsu.hino@gmail.com>

References

B. Kegl. Intrinsic dimension estimation using packing numbers. *Advances in Neural Information Processing Systems* 15, 2002.

K. W. Pettis et al. An intrinsic dimensionality estimator from near neighbor information. *IEEE transactions on pattern recognition and machine intelligence*, 1979.

Examples

```
x <- gendata(DataName='SwissRoll',n=300)
estnni <- nni(x=x)
print(estnni)
```

pack

Intrinsic Dimension Estimation Using Packing Numbers.

Description

pack estimates intrinsic dimension of given dataset based on the packing number.

Usage

```
pack(x, k1 = NULL, k2 = NULL, greedy = TRUE, eps = 0.01, DM = FALSE)
```

Arguments

x	data matrix or distance matrix given by <code>as.matrix(dist(x))</code> .
k1	first radius parameter. If one of k1 or k2 is NULL, then both are automatically determined from the input data.
k2	second radius parameter.
greedy	logical. If TRUE, then a greedy algorithm is used for estimating the packing number. If FALSE, then a hierarchical clustering algorithm is used instead.
eps	accuracy parameter.
DM	whether 'x' is distance matrix or not. logical.

Details

A variant of fractal dimension called the capacity dimension is considered. The capacity dimension is defined by using the notion of covering number, which is hard to calculate in general. In this function, the packing number of the data space is used as the surrogate of the covering number. The packing number is estimated by greedy manner or by hierarchical clustering.

Value

Estimated global intrinsic dimension.

Author(s)

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References

B. Kegl. Intrinsic dimension estimation using packing numbers. Advances in Neural Information Processing Systems 15, 2002.

B. Eriksson and M. Crovella. Estimating intrinsic dimension via clustering. IEEE Statistical Signal Processing Workshop, 2012.

Examples

```
x <- gendata(DataName='SwissRoll',n=300)
estpackG <- pack(x=x,greedy=TRUE) ## estimate the packing number by greedy method
print(estpackG)
estpackC <- pack(x=x,greedy=FALSE) ## estimate the packing number by cluttering
print(estpackC)
```

side

*Higher-order Local Information Dimension Estimator.***Description**

side is a Higher-order Information Dimension Estimator, which estimates local information dimension of given dataset based on the polynomial regression with Poisson error structure.

Usage

```
side(
  x,
  maxDim = 5,
  DM = FALSE,
  local = FALSE,
  method = "disc",
  comb = "average"
)
```

Arguments

x	data matrix or distance matrix given by <code>as.matrix(dist(x))</code> .
maxDim	maximum of the candidate dimensions.
DM	whether 'x' is distance matrix or not. logical.
local	logical. If TRUE, a vector of local dimensions at each sample point is returned.
method	algorithm to estimate intrinsic dimension. 'disc' for discrete dimension estimation. 'cont' for continuous dimension estimation with MLE by Newton-method.
comb	'average', 'median' or 'vote' for combining local estimates when global estimate is required.

Details

A variant of fractal dimension called the local information dimension is considered. The local information dimension is estimated by using the probability mass function. The function side considers higher-order expansion of the probability mass around the inspection point, and it estimates the local information dimension by fitting a generalized linear model with Poisson error structure and an identity link function. There are two methods for dimension estimation: the first method tries different dimensions and adopt the one with maximum likelihood, while the second method directly maximises the likelihood with respect to the intrinsic dimension. The former returns an

integer-valued dimension estimate, and the latter returns a real-valued estimate. The result of the former method is used as an initial value for the latter method in numerical optimization. Slow but more accurate than `mada` in some cases.

Value

Estimated local or global intrinsic dimension.

Author(s)

Hideitsu Hino <hideitsu.hino@gmail.com>

References

H. Hino, J. Fujiki, S. Akaho, and N. Murata, 'Local Intrinsic Dimension Estimation by Generalized Linear Modeling', *Neural Computation*, 2017

Examples

```
## local intrinsic dimension estimate
tmp <- gendata(DataName='ldbl', n=300)
x <- tmp$x
set.seed(999)
idx <- c(sample(which(tmp$tDim==1)[1:10],3), sample(which(tmp$tDim==2)[1:30],3))
estmada <- mada(x=x[1:100,], local=TRUE)
estmada[idx] ## estimated local intrinsic dimensions by mada
tmp$tDim[idx] ## true local intrinsic dimensions
estside <- side(x=x[1:100,], local=TRUE)
estside[idx] ## estimated local intrinsic dimensions by side
```

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